

Boron-Based Organometallic Nanostructures: Hydrogen Storage Properties and Structure Stability

Yufeng Zhao,^{*,†} Mark T. Lusk,[‡] Anne C. Dillon,[†] Michael J. Heben,[†] and Shengbai B. Zhang[†]

National Renewable Energy Laboratory, Golden, Colorado 80401, and Colorado School of Mines, Colorado 80401

Received September 10, 2007; Revised Manuscript Received November 12, 2007

ABSTRACT

Transition-metal (TM) boride and carbide nanostructures are studied as model organometallic materials for hydrogen storage. The dispersed TM atoms function as H₂ sorption centers on the surface of the boron or carbon–boron substrate. The flexibility offered in the variety of possible structures permits the study of the effect of the TM–TM distance on the storage capacity. When the TMs are too close to one another, TM–TM bonding reduces the capacity. Even when separated by distances larger than the normal TM–TM bond length, delocalization of TM valence electrons can still lower the hydrogen capacity. An optimal TM–TM distance for the structural motifs studied here is ~6 Å. Our study also permitted the evaluation of new TM boride nanostructures. We predict a low-energy single-walled scandium triboride (ScB₃) nanotube that can bind ~6.1 wt % hydrogen with a binding energy of 22~26 kJ/mol.

Introduction. Recent theoretical demonstrations of high-capacity, ambient-temperature, reversible hydrogen sorption using transition metals (TMs) complexed to carbon frameworks^{1,2} have prompted many new designs for hydrogen storage materials (HSMs).^{3–12} Experimental investigations of such complexes have already been undertaken,^{13,14} and substantial enhancement of dihydrogen binding has been shown in reduced microporous titanium oxides and Ti-doped silica.^{15,16}

The original proposals predicted high reversible capacities for isolated TM atoms supported on carbon superstructures. The stability of the arrangements have been considered a weakness in the design,¹⁷ but molecular dynamics simulations with boron substitution indicated that structural integrity would be maintained to at least 1000 K.¹ A related Li₁₂C₆₀ cluster arrangement was proposed to be more stable;¹⁸ unfortunately, the binding energy of H₂ to Li₁₂C₆₀ is too low for practical application, and the Li atoms will likely cluster once the Li₁₂C₆₀ forms within a bulk setting.^{19,20}

Stimulated by the idea that boron atoms in the substrate may stabilize the dispersed array of TM atoms,¹ Meng et al. recently proposed a metal–diboride nanotube²¹ as a means to lock the TM atoms in place. In this case, charge transfer from the TM atoms to the boron atoms causes the formation of a layered honeycomb network analogous to graphene. Boron can also form a great variety of organometallic

structures with TMs and carbon atoms, such as the so-called metallocarboranes²² and metal carborides,²³ so it is interesting to consider other ways of complexing TMs with boron and carbon.

Because dispersed TM atoms in organometallic HSMs function as hydrogen sorption centers, it is natural to consider how the density of TM atoms on the substrate affects the hydrogen storage capacity. For example, one may ask: Does the hydrogen capacity increase as the TM density increases? Interestingly, the TM–diboride nanostructures^{21,24–27} with a relatively high TM density do not provide a higher hydrogen capacity²¹ as compared to the organometallic buckyballs.¹ This suggests that a closer investigation of the relationship between TM density and hydrogen capacity is warranted.

In this study, we show that TM atoms, Sc and Ti, can bind externally to fullerene-like cages of the general formula C_xB_{60-x} ($x = 0, 36$). Because the TM–TM distance is tuned by varying x , we can investigate how the hydrogen capacity depends on the surface density of TM atoms. We also show that the metal-coated boron cages are metastable, whereas a type of Sc-embedded ScB₃ nanotube has a much lower energy and good properties for hydrogen storage. Furthermore, following analogies to nanostructures that are known to exist, we suggest that some of these new nanomaterials may be readily synthesized.

Theory and Computational Details. The gravimetric capacity, C_w , of an HSM is related to the number of sorption centers per unit HSM mass, D_s , through the number of H

* Corresponding author. E-mail: yufeng_zhao@nrel.gov.

[†] National Renewable Energy Laboratory.

[‡] Department of Physics, Colorado School of Mines.

species (n_{H} , in either atomic or molecular forms) bound to a sorption center and the atomic mass of the hydrogen atom, m_{H} , as the following:

$$C_{\text{W}} = D_{\text{s}} n_{\text{H}} m_{\text{H}} \quad (1)$$

Focusing on organometallic HSMs with TM atoms acting as sorption centers, we consider the 18-electron rule where the number of H species bound to each TM atom is

$$n_{\text{H}} = 18 - n_{\text{v}}^{\text{e}} - n_{\text{s}}^{\text{e}} - n_{\text{m}}^{\text{e}} \quad (2)$$

where the number of valence electrons in the free TM atom, n_{v}^{e} , is a constant once the TM is chosen, and n_{s}^{e} and n_{m}^{e} are the number of electrons contributed to the TM orbitals by, respectively, the substrate and neighboring TM atoms. When the TM atoms are bound to the substrate in a stable configuration, n_{s}^{e} is also a constant. However, n_{m}^{e} is affected by the TM–TM distance and hence by the TM density D_{s} . When the TM atoms are far away from one another, n_{m}^{e} can be neglected and C_{W} increases with increasing D_{s} . When TMs are close to one another, neighboring TMs interact and n_{m}^{e} is the number of TM–TM bonds. Obviously, TM separation is desired to avoid a situation in which the TM orbitals are involved in forming TM–TM bonds such that n_{H} is small. However, it is unclear how the TM–TM interaction affects hydrogen capacity in the intermediate range of TM–TM distances, which is longer than their normal bonds but shorter than that of complete separation.

An investigation of the TM density requires changing the ratio of the TM atoms to the substrate atoms. If we assume that each boron atom requires one electron to form a carbon-like electronic shell, the metal–boron stoichiometric ratio can take on several different values spanning from the 1:2 ratio investigated by Meng et al.²¹ to 1:3 or 1:4 due to the different TM valences. For example, ScB_3 and TiB_4 could be stable in nanoparticles in which the TM density is lowered. The TM density could be further lowered if carbon atoms are introduced. These considerations lead to several new nanostructured HSMs.

We used the spin-polarized first-principles density functional theory method implemented in the Vienna ab initio simulation package.²⁸ A plane-wave basis set (400 eV cutoff) was used in combination with an all-electronlike projector-augmented wave potential and Perdew–Burke–Ernserhof exchange correlation functional within the generalized gradient approximation.²⁹ The periodic, cubic unit-cell is given a dimension of 25 Å to maintain sufficient vacuum around the nanoparticles. For the one-dimensional nanotubes, the axial period is optimized in the total-energy calculation. The optimized structures are considered as equilibrium when the maximum force acting on the atoms decreases below 0.03 eV/Å. The definition of the binding energy of hydrogen can be found in refs 1 and 9.

Results and Discussion. We first calculate the metal–triboride nanocages $\text{Sc}_{20}\text{B}_{60}$ and $\text{Ti}_{20}\text{B}_{60}$ with each TM (Sc or Ti) atom sitting on top of the center of a hexagonal ring,

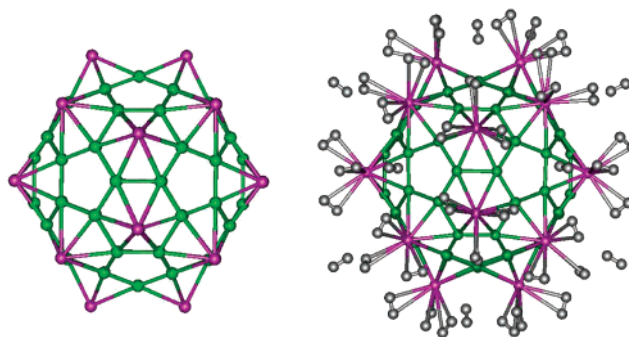


Figure 1. A metal-boride buckyball $\text{Sc}_{20}\text{B}_{60}$ (left) adsorbs 72 H_2 or 8.6 wt % (right). Each Sc atom binds three H_2 , and each pentagon ring binds one H_2 . Green and pink balls are B and Sc atoms, respectively.

Table 1. HOMO–LUMO Gaps for the Nanoparticles before and after Hydrogen Charging

structure	gap (eV)	structure	gap (eV)
$\text{Ti}_{20}\text{B}_{60}$	0.02	$\text{Sc}_{20}\text{B}_{60}$	0.20
$\text{H}_{104}\text{Ti}_{20}\text{B}_{60}$	0.28	$\text{H}_{144}\text{Sc}_{20}\text{B}_{60}$	0.27
$\text{Ti}_{12}\text{B}_{24}\text{C}_{36}$	0.06	$\text{Sc}_{12}\text{B}_{24}\text{C}_{36}$	0.12
$\text{H}_{132}\text{Ti}_{12}\text{B}_{24}\text{C}_{36}$	1.43	$\text{H}_{144}\text{Sc}_{12}\text{B}_{24}\text{C}_{36}$	1.48

Table 2. Hydrogen Storage Property of Metal–Boride and Metal–Carbide Nanostructures

structure	TM–TM distance (Å)	H_2 binding (kJ/mol)	capacity (wt %)
TiB_2 tube ^a	3.0–3.3	19–58	5.5
$\text{TiB}_3(\text{Ti}_{20}\text{B}_{60})$	3.69	12–36	6.5
$\text{TiB}_2\text{C}_3(\text{Ti}_{12}\text{B}_{24}\text{C}_{36})$	5.47	38	8.6
$\text{ScB}_3(\text{Sc}_{20}\text{B}_{60})$	3.84	15–25	8.6
$\text{ScB}_2\text{C}_3(\text{Sc}_{12}\text{B}_{24}\text{C}_{36})$	5.62	39	10.5

^a Taken from ref 21.

Notice that if the TM atoms are replaced with B atoms, these structures change into the recently predicted B_{80} fullerene.³⁰ Note that $\text{Sc}_{20}\text{B}_{60}$ has exactly the same I_{h} symmetry and the same number of valence electrons as B_{80} . Figure 1 (left) shows the optimized structure of the $\text{Sc}_{20}\text{B}_{60}$ metal–triboride buckyball. In this case, each Sc atom can bind three H_2 ligands (Figure 1, right) with a binding energy of 25.1 kJ/mol H_2 . In addition to the H_2 molecules bound to the Sc atoms, one extra H_2 can bind on top of a pentagonal ring with a binding energy of 15.4 kJ/mol H_2 . In $\text{Ti}_{20}\text{B}_{60}$, each Ti atom binds two H_2 (35.6 kJ/mol H_2), and one more H_2 is bound (11.6 kJ/mol H_2) to each pentagon. The highest occupied molecular orbital–lowest unoccupied molecular orbital (HOMO–LUMO) gap of $\text{Sc}_{20}\text{B}_{60}$ is 10 times larger than that of $\text{Ti}_{20}\text{B}_{60}$ (Table 1), indicating that the electron-counting rule requires roughly one electron being transferred to each B atom from the metal atoms.

Although the density of the TM atoms is lower than in TiB_2 nanotubes,²¹ these nanostructures store more hydrogen (see Table 2). Notice that the TM–TM distance (~ 3.8 Å) in $\text{Sc}_{20}\text{B}_{60}$ and $\text{Ti}_{20}\text{B}_{60}$ is larger than that in the TiB_2 nanotubes (3.0–3.3 Å). The question then arises: Can the hydrogen capacity be increased if the TM–TM distance is

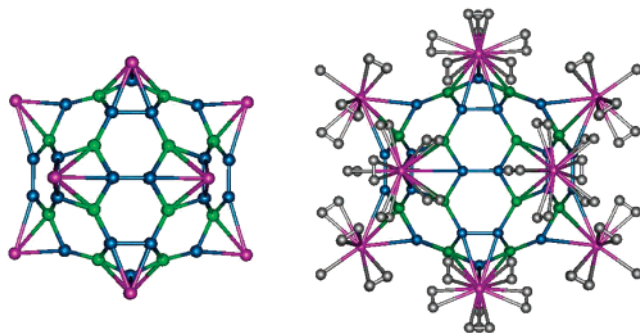


Figure 2. A metal–carboride buckyball $\text{Sc}_{12}\text{B}_{24}\text{C}_{36}$ (left) adsorbs 72 H_2 or 10.5 wt % (right). Each Sc atom binds six H_2 . Green, blue, and pink balls are B, C, and Sc atoms, respectively.

further enlarged? The TM–TM distance might be increased by simply removing TM atoms, but this would lead to destabilization of the boron cage because boron atoms prefer a high coordination number when there is not sufficient electron donation from metal atoms. Another approach is to replace some of the boron atoms with carbon. This approach appears to be viable because the energetic and thermodynamic favorability of metal carborides has been shown in experimental work.^{22,23}

Figure 2 shows a metal–carboride buckyball, $\text{Sc}_{12}\text{B}_{24}\text{C}_{36}$, in which each Sc atom covers a pentagonal ring with three C atoms and two B atoms. This can be considered a heavily B-doped C_{60} with Sc decoration. In $\text{Sc}_{12}\text{B}_{24}\text{C}_{36}$, each Sc atom binds as many as six H_2 with an average binding energy of 38.6 kJ/mol H_2 . We also calculated the structural analog for Ti, that is, $\text{Ti}_{12}\text{B}_{24}\text{C}_{36}$, and found that each Ti atom can bind one hydride and five H_2 . The binding energy of the hydride (179 kJ/mol H_2) is too high for the H atoms to be retrieved at ambient conditions but that of the dihydrogen (37.6 kJ/mol H_2) is nearly ideal. Compared with the $\text{M}_{20}\text{B}_{60}$ ($\text{M} = \text{Sc}, \text{Ti}$) case, the hydrogen capacity in $\text{M}_{12}\text{B}_{24}\text{C}_{36}$ is increased though the metal density is decreased.

These results indicate that the distance between TM centers is a key factor in the design of optimal organometallic HSMs. Table 2 summarizes the relationship between the TM–TM distances and the capacity within the structural motifs investigated here. It is seen that the hydrogen capacity increases with TM–TM distance. However, this will not be a monotonic trend in the limit, because a low density of metal atoms will eventually reduce the hydrogen uptake per unit mass of HSM, as expected from eq 1.

One might conjecture that the relatively low capacity at high metal density is mainly due to steric effects associated with the metal species being too close.²¹ However, this cannot explain why $\text{Ti}_{20}\text{B}_{60}$ stores less hydrogen than $\text{Sc}_{20}\text{B}_{60}$ where the metal–metal separation is similar. We found that the degree of electron localization plays a key role. Even at a TM–TM distance much longer than their direct bonds, the TM atoms tend to interact with each other through valence-electron delocalization mediated by the substrate. Because Ti has one more valence electron than Sc, the delocalization effect in $\text{Ti}_{20}\text{B}_{60}$ is more pronounced than in $\text{Sc}_{20}\text{B}_{60}$, and this is reflected in the gaps listed in Table 1. Figure 3 shows

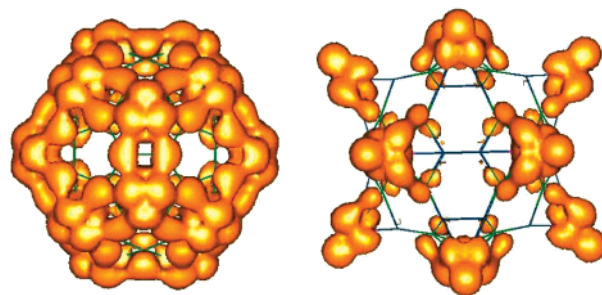


Figure 3. Charge density of the highest occupied band for $\text{Ti}_{20}\text{B}_{60}$ (left) and $\text{Ti}_{12}\text{B}_{24}\text{C}_{36}$ (right) nanoparticles.

the highly delocalized electronic states in the highest occupied band of $\text{Ti}_{20}\text{B}_{60}$. TM valence electrons are delocalized in both $\text{Sc}_{20}\text{B}_{60}$ and $\text{Ti}_{20}\text{B}_{60}$ due to an intermediate TM–TM distance of 3.7–3.8 Å. In contrast, as the TM–TM distance increases further to 5.5–5.6 Å in $\text{Ti}_{12}\text{B}_{24}\text{C}_{36}$ and $\text{Sc}_{12}\text{B}_{24}\text{C}_{36}$, the TM valence electrons are highly localized around the pentagonal rings (Figure 3). Such an electronic effect is also reflected in the chemistry of the nanoparticles. As shown in Table 1, the fully charged $\text{Ti}_{20}\text{B}_{60}$ and $\text{Sc}_{20}\text{B}_{60}$ species (i.e., $\text{H}_{104}\text{Ti}_{20}\text{B}_{60}$ and $\text{H}_{144}\text{Sc}_{20}\text{B}_{60}$) have a much narrower gap than the fully charged $\text{Sc}_{12}\text{B}_{24}\text{C}_{36}$ and $\text{Ti}_{12}\text{B}_{24}\text{C}_{36}$ (i.e., $\text{H}_{132}\text{Ti}_{12}\text{B}_{24}\text{C}_{36}$ and $\text{H}_{144}\text{Sc}_{12}\text{B}_{24}\text{C}_{36}$), which implies that $\text{H}_{104}\text{Ti}_{20}\text{B}_{60}$ and $\text{H}_{144}\text{Sc}_{20}\text{B}_{60}$ are chemically unsaturated. The electron delocalization does not fully saturate the TM orbitals, yet the hydrogen capacity is significantly reduced. Notice that in $\text{H}_{132}\text{Ti}_{12}\text{B}_{24}\text{C}_{36}$ and $\text{H}_{144}\text{Sc}_{12}\text{B}_{24}\text{C}_{36}$ the TM atom, H_2 molecules, and H atoms satisfy the 18-e rule in each pentagonal ring and create local aromaticity. The hydrogen capacity reaches its maximum at a TM–TM distance of ~6 Å, which should be near the optimized value.

To evaluate the stability of the nanostructures, we calculated the energies of the $\text{Sc}_{20}\text{B}_{60}$ isomers with some of the Sc atoms moved into the B_{60} cage. This may be considered as a perturbation to the targeted structure. Figure 4 shows that the total energy drops by 0.58, 1.15, and 6.29 eV with 1, 2, and 4 Sc moved inside, respectively. Extending this type of study to the TiB_2 tube, we may expect similar results because TM atoms favor higher coordination numbers. As more TM atoms go inside the tube (or cage), the structure should collapse and form a solid particle. However, there are some hollow structures that are stable when boron is coordinated with five neighbors. For example, we have found an exceptionally stable nanotube of formula ScB_3 in which the Sc atoms are embedded in the wall and all the boron atoms have 5-fold coordination, as shown in Figure 5 (lower panel). In this fully relaxed structure with an axial period of 5.90 Å, the nearest B–B, B–Sc, and Sc–Sc distances are 1.61, 2.43, and 3.48 Å, respectively. Our calculation shows that the energy of the Sc-embedded ScB_3 nanotube is 0.8 eV lower per ScB_3 unit than the Sc-coated one (Figure 5, upper panel). Compared to the $\text{Sc}_{20}\text{B}_{60}$ buckyball in Figure 1 and its lowest-energy solid isomer (in Figure 4 with four Sc inside), the Sc-embedded ScB_3 nanotube is 0.60 and 0.29 eV lower, respectively, in total energy per ScB_3 unit. This implies that a variety of cage-like TM boride nanostructures may exist.

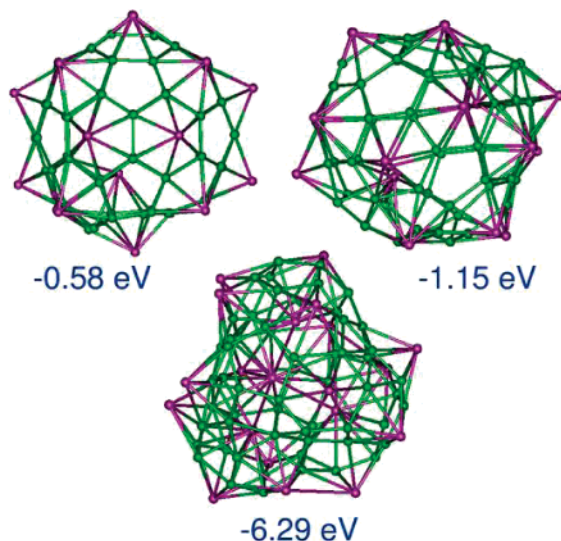


Figure 4. Three $\text{Sc}_{20}\text{B}_{60}$ isomers with 1, 2, and 4 of the 20 Sc atoms inside the B_{60} . Their total energies are 0.58, 1.15, and 6.29 eV lower, respectively, than the Sc-coated B_{60} (as shown in Figure 1).

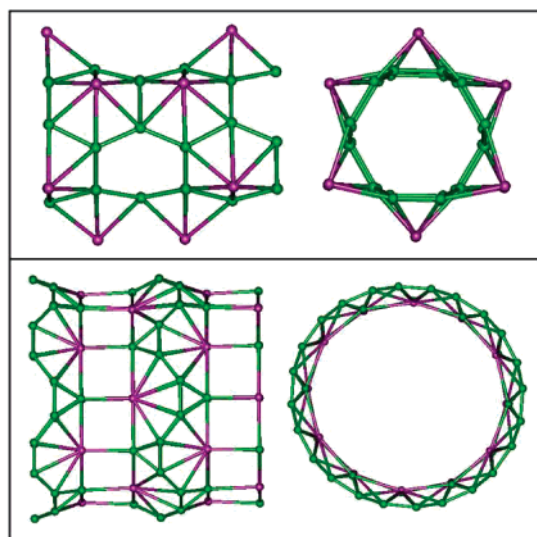
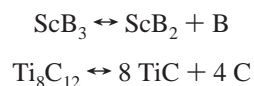


Figure 5. Predicted Sc-coated (upper panel) and Sc-embedded (lower panel) ScB_3 nanotubes. Side views and axial views are shown. The total energy of the Sc-embedded nanotube is 0.8 eV lower per stoichiometric unit (ScB_3) than the Sc-coated one.

To further evaluate the feasibility of synthesis of the Sc-embedded ScB_3 nanotube, we compare here the formation energy of this ScB_3 nanotube with the famous Ti_8C_{12} MetCar molecule, via the following reactions:



The formulas on the left-hand side are nanostructures, and those on the right-hand side represent bulk materials from which the nanostructures are formed. The well-known scandium diboride (ScB_2) and the titanium carbide (TiC) are, respectively, hexagonal closed packed HCP-A3 and rock salt

B1 crystals. Bulk boron is the ground-state β -boron (R-105), and the bulk carbon is graphene. According to our calculation, the formation energy of the predicted ScB_3 nanotube is 0.64 eV per atom as in comparison with that of 1.02 eV per atom of Ti_8C_{12} molecules. Notice that the formation energy of C_{60} is ~ 0.4 eV per carbon atom with respect to graphene;³¹ this implies a high possibility of existence of the ScB_3 nanotubes. As for the synthesis of $\text{M}_{12}\text{B}_{24}\text{C}_{36}$, the problem is similar to B substitution of C in small hydrocarbon molecules in the presence of metal.²² For example, the sandwiched organometallic structures containing $[\text{C}_3\text{B}_2\text{H}_5]^{2-}$ carborane²² could be precursors for synthesis of TM-coated $\text{B}_{24}\text{C}_{36}$ buckyballs.

We also investigated the interaction of the Sc-embedded ScB_3 nanotube with hydrogen. Our calculation shows that each boron atom binds one atomic H, and each Sc atom binds one dihydrogen molecule through Kubas coordination, resulting in a total hydrogen capacity of 6.1 wt %. Interestingly, the binding energy of the atomic hydrogen (22 kJ/mol H_2) is slightly smaller than that of the dihydrogen, 26 kJ/mol H_2 . This means that both these two types of hydrogen can be reversibly charged/discharged at near ambient condition. The hydrogenation/dehydrogenation of boron atoms may be catalyzed by the Sc atom, as has been shown for MetCars.⁹

Conclusion. In summary, we investigated the effect of TM density on hydrogen storage in organometallic structures. Undercoordinated surface TM atoms can interact through surface delocalization of valence electrons, which can lower the hydrogen capacity. There exists an optimal TM–TM distance (~ 6 Å) for the maximum hydrogen capacity in organometallic frameworks with dispersed TM atoms. Finally, stable single-walled ScB_3 nanotubes are predicted that show potential for hydrogen storage.

Acknowledgment. This work is supported by the Office of Energy Efficiency and Renewable Energy Hydrogen, Fuel Cell, and Infrastructure Technologies Program of the Department of Energy through the Hydrogen Sorption Center of Excellence under Grant DE-AC36-99GO10337. We thank H.-J. Xiang for helpful suggestions.

References

- (1) Zhao, Y.; Kim, Y.-H.; Dillon, A. C.; Heben, M. J.; Zhang, S. B. *Phys. Rev. Lett.* **2005**, *94*, 155504.
- (2) Yildirim, T.; Ciraci, S. *Phys. Rev. Lett.* **2005**, *94*, 175501.
- (3) Gagliardi, L. *J. Chem. Theory Comput.* **2005**, *1*, 1172–1175.
- (4) Shin, W. H.; Yang, S. H.; Goddard, W. A.; Kang, J. K. *Appl. Phys. Lett.* **2006**, *88*, 053111.
- (5) Lee, H.; Choi, W. I.; Ihm, J. *Phys. Rev. Lett.* **2006**, *97*, 056104.
- (6) Du, A. J.; Smith, S. C.; Yao, X. D.; Lu, G. Q. *J. Phys. Chem. B* **2006**, *110*, 21747–21750.
- (7) Weck, P. F.; Kumar, T. J. D.; Kim, E.; Balakrishnan, N. *J. Chem. Phys.* **2007**, *126*, 094703–6.
- (8) Wu, X. J.; Yang, J. L.; Zeng, X. C. *J. Chem. Phys.* **2006**, *125*, 044704.
- (9) Zhao, Y. F.; Dillon, A. C.; Kim, Y. H.; Heben, M. J.; Zhang, S. B. *Chem. Phys. Lett.* **2006**, *425*, 273–277.
- (10) Durgun, E.; Ciraci, S.; Zhou, W.; Yildirim, T. *Phys. Rev. Lett.* **2006**, *97*, 226102.
- (11) Park, N.; Hong, S.; Kim, G.; Jhi, S. H. *J. Am. Chem. Soc.* **2007**, *129*, 8999–9003.
- (12) Zhao, Y. F.; Heben, M. J.; Dillon, A. C.; Simpson, L. J.; Blackburn, J. L.; Dorn, H. C.; Zhang, S. B. *J. Phys. Chem. C* **2007**, *111*, 13275–13279.

- (13) Borchers, C.; Khomenko, T. I.; Morozova, O. S.; Galakhov, A. V.; Kurmaev, E. Z.; McNaughton, J.; Yabloskikh, M. V.; Moewes, A. *J. Phys. Chem. B* **2006**, *110*, 196–204.
- (14) Wang, X. L.; Tu, J. P. *Appl. Phys. Lett.* **2006**, *89*, 064101.
- (15) Hu, X.; Skadtchenko, B. O.; Trudeau, M.; Antonelli, D. M. *J. Am. Chem. Soc.* **2006**, *128*, 11740–11741.
- (16) Hu, X.; Trudeau, M.; Antonelli, D. M. *Chem. Mater.* **2007**, *19*, 1388–1395.
- (17) Sun, O.; Wang, Q.; Jena, P.; Kawazoe, Y. *J. Am. Chem. Soc.* **2005**, *127*, 14582–14583.
- (18) Sun, Q.; Jena, P.; Wang, Q.; Marquez, M. *J. Am. Chem. Soc.* **2006**, *128*, 9741–9745.
- (19) Buhl, M. Z. *Anorg. Allg. Chem.* **2000**, *626*, 332–337.
- (20) Cristofolini, L.; Facci, P.; Fontana, M. P.; Cicognani, G.; Dianoux, A. *J. Phys. Rev. B* **2000**, *61*, 3404–3409.
- (21) Meng, S.; Kaxiras, E.; Zhang, Z. *Nano Lett.* **2007**, *7*, 663–667.
- (22) Grimes, R. N. *Chem. Rev.* **1992**, *92*, 251–268.
- (23) Kriz, O.; Rheingold, A. L.; Shang, M. Y.; Fehlner, T. P. *Inorg. Chem.* **1994**, *33*, 3777–3783.
- (24) Ivanovskaya, V.; Enjashin, A. N.; Sofronov, A. A.; Makurin, Y. N.; Medvedeva, N. I.; Ivanovskii, A. L. *J. Mol. Struct.* **2003**, *625*, 9–16.
- (25) Nagamatsu, J.; Nakagawa, N.; Muranaka, T.; Zenitani, Y.; Akimitsu, J. *Nature* **2001**, *410*, 63–64.
- (26) Quandt, A.; Liu, A. Y.; Boustani, I. *Phys. Rev. B* **2001**, *64*, 6412.
- (27) Zhang, P. H.; Crespi, V. H. *Phys. Rev. Lett.* **2002**, *89*, 056403.
- (28) Kresse, G.; Furthmüller, J. *Phys. Rev. B* **1996**, *54*, 11169–11186.
- (29) Perdew, J. P.; Burke, K.; Ernzerhof, M. *Phys. Rev. Lett.* **1996**, *77*, 3865–3868.
- (30) Szvacki, N. G.; Sadrzadeh, A.; Yakobson, B. I. *Phys. Rev. Lett.* **2007**, *98*, 166804.
- (31) Chen, H. S.; Kortan, A. R.; Haddon, R. C.; Kaplan, M. L.; Chen, C. H.; Mujsce, A. M.; Chou, H.; Fleming, D. A. *Appl. Phys. Lett.* **1991**, *59*, 2956–2958.

NL072321F