



DMREF/Collaborative Research: Nitride Discovery - Creating the Knowledge Base for Hard Coating

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NSF: CMMI, CNS; Ohio Supercomputer Center, PVIC, U. of Toledo

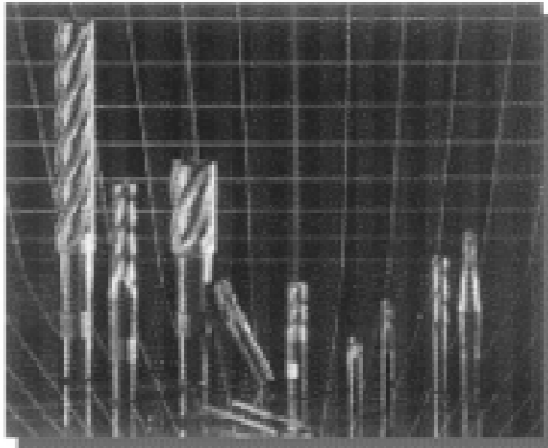


Outline

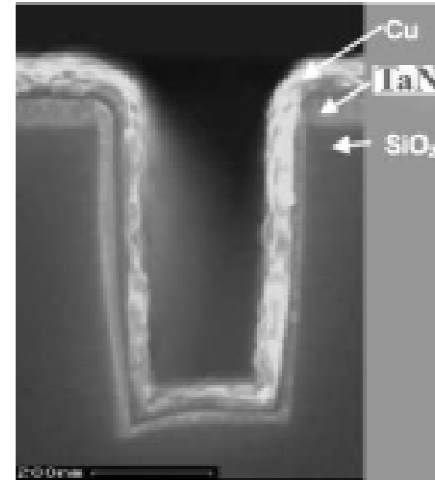
- Transition metal nitrides (TMNs)
- Coatings By Design Approach
- Experimental approaches
- Theoretical Approaches
- *Ab initio* method
- Results for Cubic structures – zincblende, rocksalt, CsCl, NbO
- Structural, mechanical and electronic properties
 - Lattice constants and bulk modulus (B)
 - Elastic constants, C_{11} , C_{12} , C_{44}
 - Ductility indicators
 - Vicker's hardness (H_V)
 - Correlation of H_V with θ_D
 - Correlation of H_V with TDOS
 - LDOS
 - Bader analysis
- Conclusion
- Future



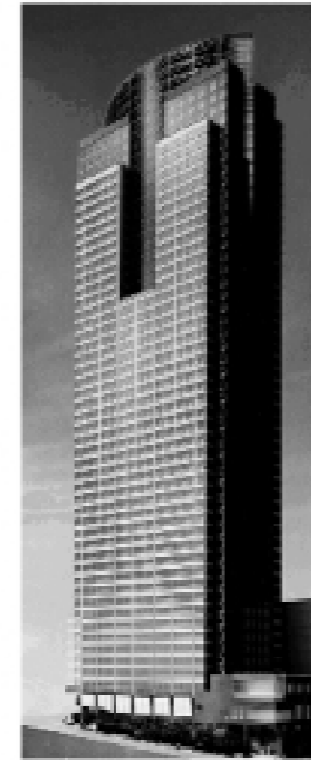
Transition-metal nitrides: applications



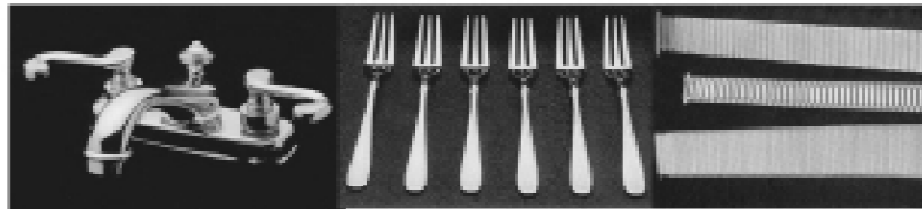
Hard wear-resistant coatings
(TiN, ZrN, CrN, TaN)



Diffusion barriers
(TiN, TaN)



Optical coatings
(TiN, ZrN)



Decorative coatings (TiN, ZrN)



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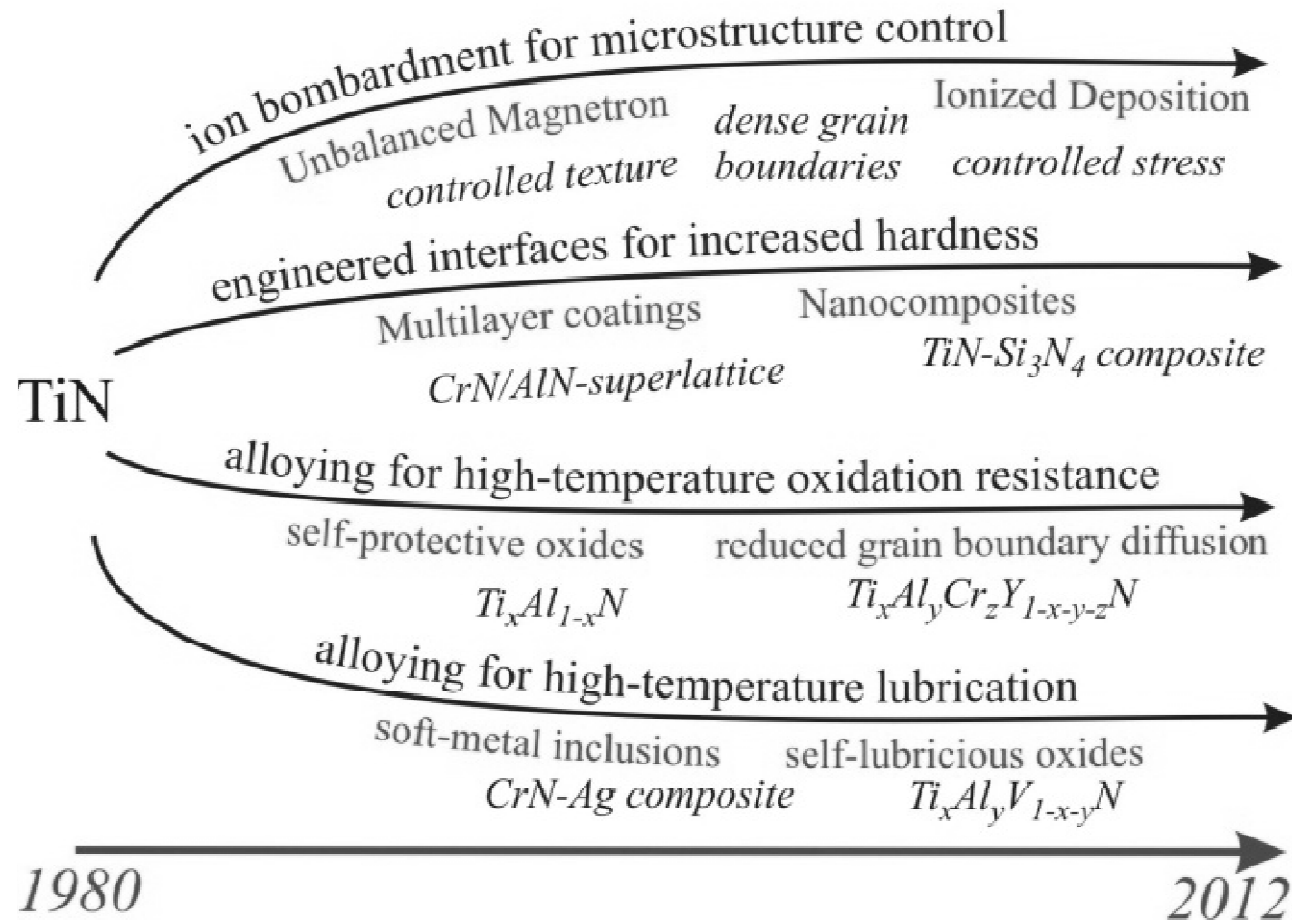


Transition Metal Nitrides (TMNs)

- Refractory hard materials
- Extremely high hardness – wear resistance
- High melting points – thermal resistance
- Good electrical and thermal conductivity
- Good corrosion resistance



Evolutionary Development of Nitride Hard Coatings





Coatings by Design

Knowledge Base I: Intrinsic Properties of Single Crystal Nitrides

properties of
binary nitrides

anisotropy of
intrinsic properties

properties of solid solutions:
ternary, quaternary nitrides

effect of off-stoichiometry effect of
uniform stress

Knowledge Base II: Microstructure Effects on Physical Properties

grain size and shape

grain boundaries

congruent interface between
two nitrides

random interface between
dissimilar nitrides

microstructural anisotropy

2. Coating Synthesis:

development of deposition technique/parameters
to create desired composition and microstructure



Knowledge Base II

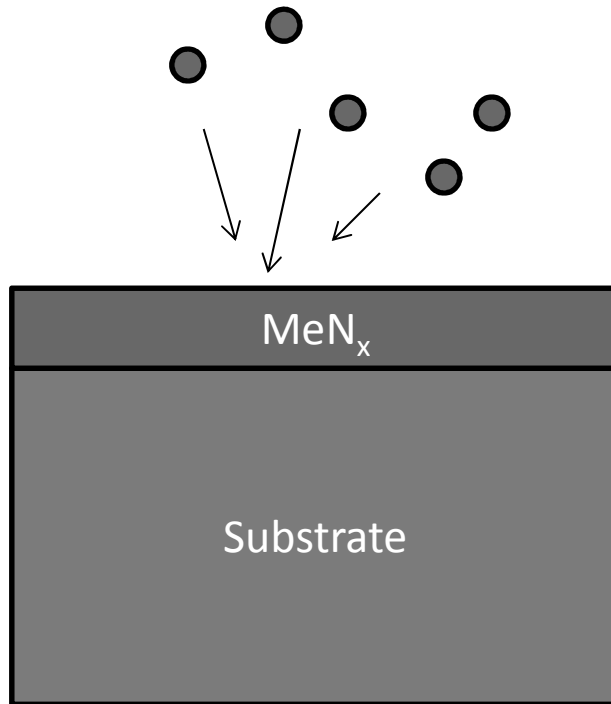
Microstructure Effects on Physical Properties

Experimental work of Prof. Daniel Gall at RPI



Experimental Approach

Brian Ozsdolay and Daniel Gall
Rensselaer Polytechnic Institute



Epitaxial layer deposition
by reactive magnetron sputtering

Measurement of properties:

- Lattice constants
- Elastic constants
- Mechanical properties
- Temperature stability
- Oxidation stability

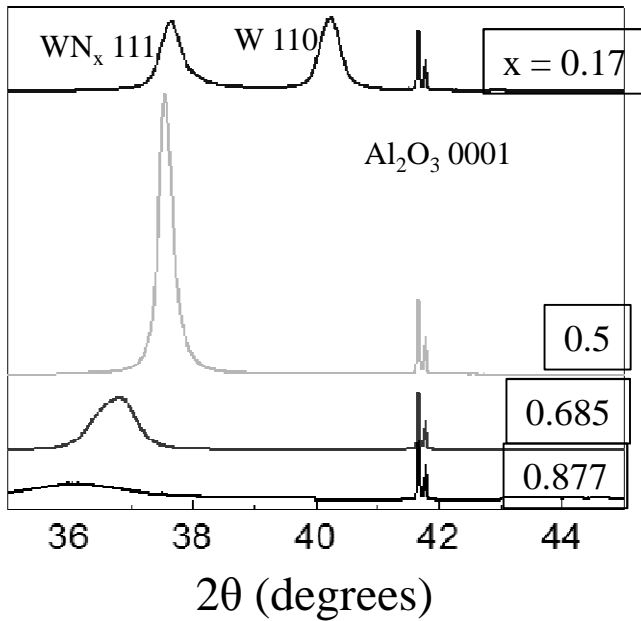


First studied material system: WN_x

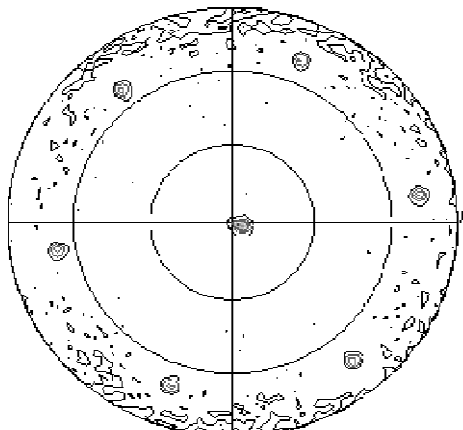
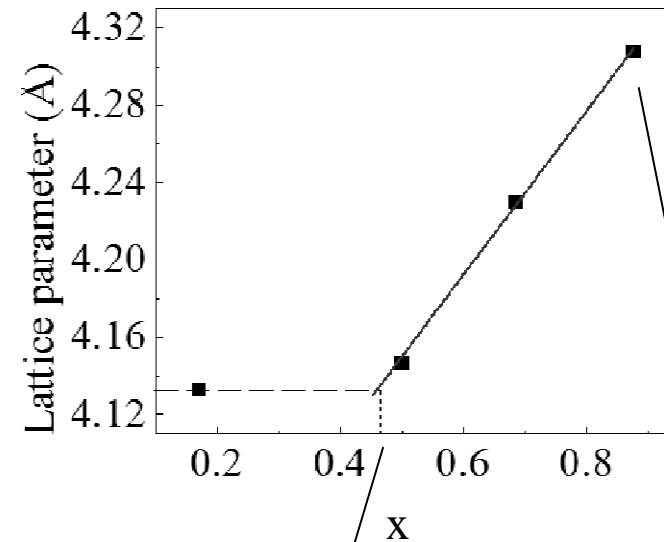


X-ray Diffraction

Lattice constant vs composition

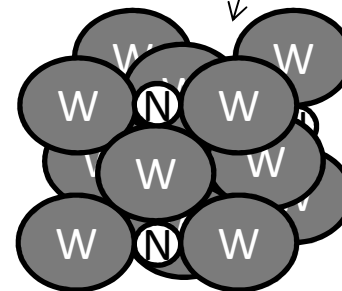


WN_x lattice parameter vs x

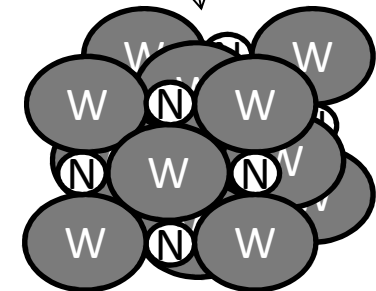


111 pole figure

WN (111) || Al₂O₃ (0001)
 WN <110> || Al₂O₃ <11̄20>



x = 0.45



x = 1

→ WN_x is epitaxial (two domains)

→ Large single phase field in WN_x (~0.45 < x < 1)

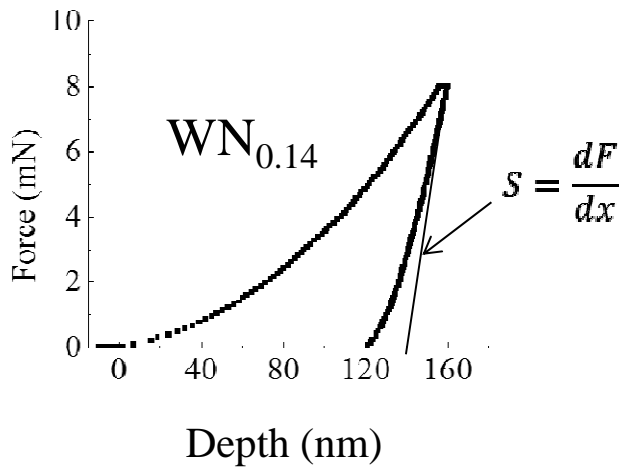


Mechanical Properties Measurements



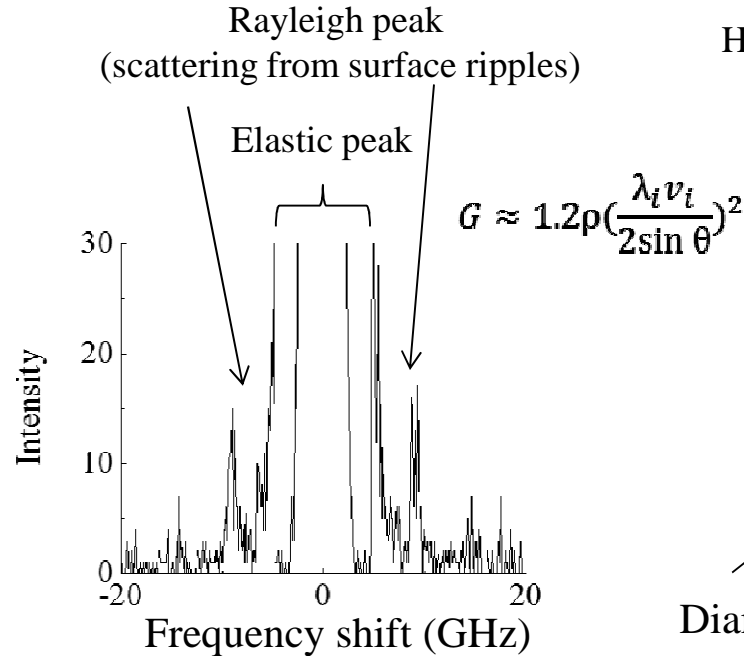
Nanoindentation

$$H = \frac{F}{A} \quad E_r = \frac{\sqrt{\pi} S}{2 \sqrt{A}}$$



- Hardness
- Elastic modulus

Surface Brillouin Scattering (SBS)



- Shear modulus
- C_{11}, C_{12}, C_{44}

Diamond Anvil Cell (DAC)

High Pressure XRD and SBS
(0-10 GPa)



Diamond facet - 1mm diameter

- Bulk modulus
- Bonding asymmetry
- Phase transitions

Direct comparison to first principles calculations



Knowledge Base I

Intrinsic Properties of Single Crystal Nitrides

**Theoretical work by Sanjay V. Khare with
students Terence Liu, Xiuquan Zhou, S. K.
R. Patil and others**



The General Program

Prepare input files of a series of TMNs for DFT computations

Ab initio
computation

Lattice constant, elastic constants, DOS

Effective
medium theory

Bulk modulus, shear modulus, Young's modulus
Poisson's ratio, Pugh's ratio, Vicker's hardness

Visualization

Visualization

Recognize **trends** and **correlations** between trends
Identify promising ones and eliminate the opposite



Applicability of *Ab Initio* Methods



Pros

Very good at predicting structural properties:

- (1) Lattice constant good to 1-3%
- (2) Elastic constants good to 1-10%
- (3) Very robust relative energy ordering between structures
- (4) Good pressure induced phase changes

Good band structures, electronic properties

Good phonon spectra

Good chemical reaction and bonding pathways

Cons

Computationally intensive

Band gaps are wrong

Excited electronic states are difficult



Structural, mechanical and electronic properties of 3d transition metal nitrides in cubic zincblende, rocksalt and cesium chloride structures



Periodic Table 3d highlight

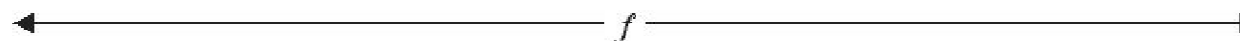
Combine with previous slide

Periodic Table
1998 Dr. Michael Blaber

1 1 H 1.008																	2 2 He 4.003
3 3 Li 6.941	4 4 Be 9.012											5 5 B 10.81	6 6 C 12.01	7 7 N 14.01	8 8 O 16.00	9 9 F 19.00	10 10 Ne 20.18
11 3 Na 22.99	12 2/IIA Mg 24.30	← VII →										13 13/IIIA Al 26.98	14 14/IVA Si 28.09	15 15/VA P 30.97	16 16/VIA S 32.07	17 17/VIIA Cl 35.45	18 18/VIIIA Ar 39.95
19 4 K 39.10	20 20 Ca 40.08	21 21 Sc 44.96	22 22 Ti 47.87	23 23 V 50.94	24 24 Cr 52.00	25 25 Mn 54.94	26 26 Fe 55.85	27 27 Co 58.93	28 28 Ni 58.69	29 29 Cu 63.55	30 30 Zn 65.39	31 31 Ga 69.72	32 32 Ge 72.61	33 33 As 74.92	34 34 Se 78.96	35 35 Br 79.90	36 36 Kr 83.80
37 5 Rb 85.47	38 38 Sr 87.62	39 39 Y 88.91	40 40 Zr 91.22	41 41 Nb 92.91	42 42 Mo 95.94	43 43 Tc 98.91	44 44 Ru 101.1	45 45 Rh 102.9	46 46 Pd 106.4	47 47 Ag 107.9	48 48 Cd 112.4	49 49 In 114.8	50 50 Sn 118.7	51 51 Sb 121.8	52 52 Te 127.6	53 53 I 126.9	54 54 Xe 131.3
55 6 Cs 132.9	56 56 Ba 137.3	La-Lu	72 72 Hf 178.5	73 73 Ta 180.9	74 74 W 183.8	75 75 Re 186.2	76 76 Os 190.2	77 77 Ir 192.2	78 78 Pt 195.1	79 79 Au 197.0	80 80 Hg 200.6	81 81 Tl 204.4	82 82 Pb 207.2	83 83 Bi 209.0	84 84 Po 210.0	85 85 At 210.0	86 86 Rn 222.0
87 7 Fr 223.0	88 88 Ra 226.0	Ac-Lr	104 104 Db	105 105 Jl	106 106 Rf	107 107 Bh	108 108 Hn	109 109 Mt	110 110 Uun	111 111 Uuu							

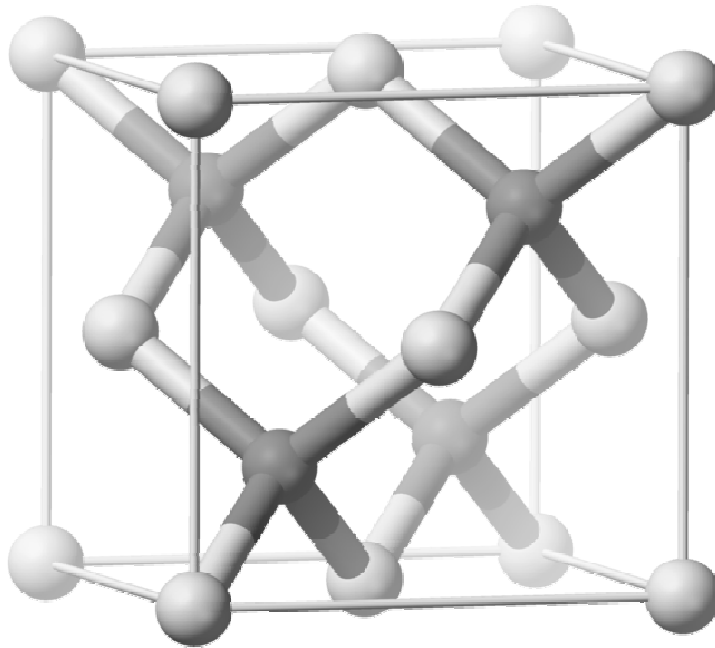


Lanthanides	57 La 138.9	58 Ce 140.1	59 Pr 140.9	60 Nd 144.2	61 Pm 146.9	62 Sm 150.4	63 Eu 152.0	64 Gd 157.2	65 Tb 158.9	66 Dy 162.5	67 Ho 164.9	68 Er 167.3	69 Tm 168.9	70 Yb 173.0	71 Lu 175.0
Actinides	89 Ac 227.0	90 Th 232.0	91 Pa 231.0	92 U 238.0	93 Np 237.0	94 Pu 239.1	95 Am 241.1	96 Cm 244.1	97 Bk 249.1	98 Cf 252.1	99 Es 252.1	100 Fm 257.1	101 Md 258.1	102 No 259.1	103 Lr 262.1





Structure – zincblende (MN)



Lattice Vectors

$$\mathbf{A}_1 = \frac{1}{2} a \mathbf{Y} + \frac{1}{2} a \mathbf{Z}$$

$$\mathbf{A}_2 = \frac{1}{2} a \mathbf{X} + \frac{1}{2} a \mathbf{Z}$$

$$\mathbf{A}_3 = \frac{1}{2} a \mathbf{X} + \frac{1}{2} a \mathbf{Y}$$

Basis Vectors

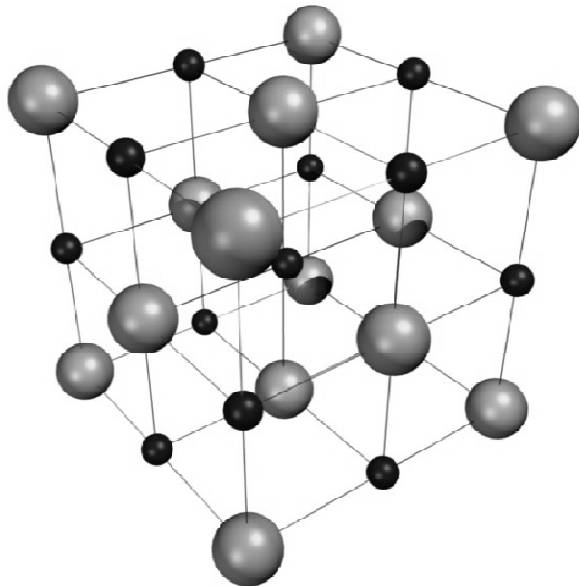
$$\mathbf{B}_1 = 0$$

$$\mathbf{B}_2 = \frac{1}{4} \mathbf{A}_1 + \frac{1}{4} \mathbf{A}_2 + \frac{1}{4} \mathbf{A}_3 = \frac{1}{4} a \mathbf{X} + \frac{1}{4} a \mathbf{Y} + \frac{1}{4} a \mathbf{Z}$$

<http://en.wikipedia.org/wiki/File:Sphalerite-unit-cell-depth-fade-3D-balls.png>



Structure – rocksalt (MN)



Lattice Vectors

$$\mathbf{A}_1 = \frac{1}{2} a \mathbf{Y} + \frac{1}{2} a \mathbf{Z}$$

$$\mathbf{A}_2 = \frac{1}{2} a \mathbf{X} + \frac{1}{2} a \mathbf{Z}$$

$$\mathbf{A}_3 = \frac{1}{2} a \mathbf{X} + \frac{1}{2} a \mathbf{Y}$$

Basis Vectors

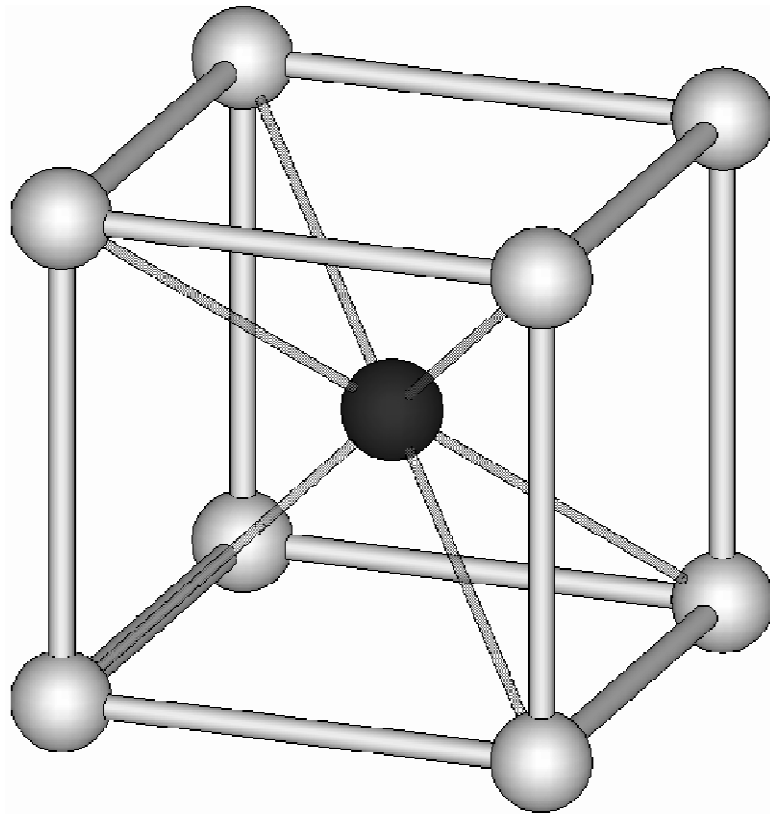
$$\mathbf{B}_1 = 0$$

$$\mathbf{B}_2 = \frac{1}{2} \mathbf{A}_1 + \frac{1}{2} \mathbf{A}_2 + \frac{1}{2} \mathbf{A}_3 = \frac{1}{2} a \mathbf{X} + \frac{1}{2} a \mathbf{Y} + \frac{1}{2} a \mathbf{Z}$$

<http://commons.wikimedia.org/wiki/File:Nacl-structure.jpg>



Structure – cesium chloride (MN)



Lattice Vectors

$$\mathbf{A}_1 = a \mathbf{X}$$

$$\mathbf{A}_2 = a \mathbf{Y}$$

$$\mathbf{A}_3 = a \mathbf{Z}$$

Basis Vectors

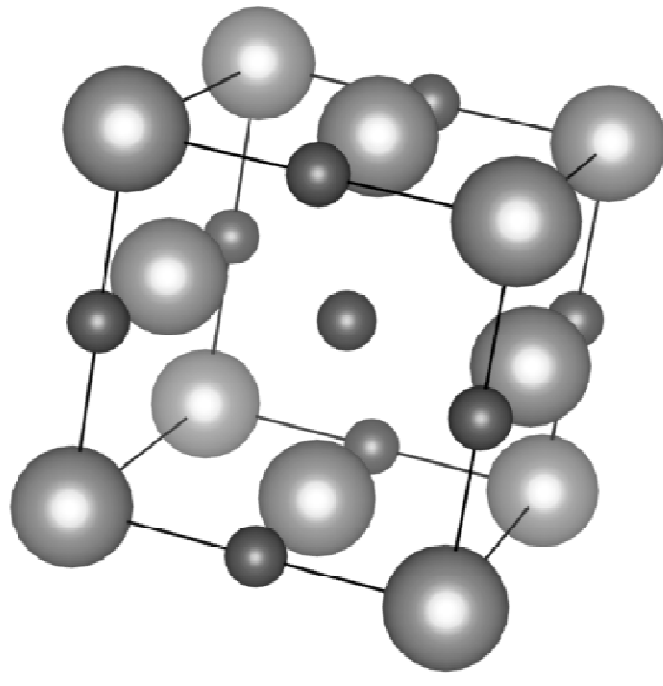
$$\mathbf{B}_1 = 0$$

$$\mathbf{B}_2 = \frac{1}{2} \mathbf{A}_1 + \frac{1}{2} \mathbf{A}_2 + \frac{1}{2} \mathbf{A}_3 = \frac{1}{2} a \mathbf{X} + \frac{1}{2} a \mathbf{Y} + \frac{1}{2} a \mathbf{Z}$$

<http://meatfighter.com/puls/>



Structure – NbO (MN)



Lattice Vectors

$$\mathbf{A}_1 = a \mathbf{X}$$

$$\mathbf{A}_2 = a \mathbf{Y}$$

$$\mathbf{A}_3 = a \mathbf{Z}$$

Basis Vectors

$$\mathbf{B}_1 = 0$$

$$\mathbf{B}_4 = \frac{1}{2} \mathbf{A}_2$$

$$\mathbf{B}_2 = \frac{1}{2} \mathbf{A}_1 + \frac{1}{2} \mathbf{A}_2$$

$$\mathbf{B}_5 = \frac{1}{2} \mathbf{A}_3$$

$$\mathbf{B}_3 = \frac{1}{2} \mathbf{A}_1 + \frac{1}{2} \mathbf{A}_3$$

$$\mathbf{B}_6 = \frac{1}{2} \mathbf{A}_1 + \frac{1}{2} \mathbf{A}_2 + \frac{1}{2} \mathbf{A}_3$$



M	a (Å)			C ₁₁ (GPa)			C ₁₂ (GPa)			C ₄₄ (GPa)			Mechanical Stability		
	zb	rs	cc	zb	rs	cc	zb	rs	cc	zb	rs	cc	zb	rs	cc
Sc	4.883	4.503	2.768	179.6	434.7	502.8	132.9	97.7	42.2	71.8	160.9	-119.2	S	S	U
		4.516 ^a			390 ^a			105 ^a			166 ^a				
		4.48 ^b			386.4 ^b			101 ^b			171.7 ^b				
		4.44 ^c													
Ti	4.569	4.221	2.607	307.2	657.7	619.6	165.2	121.0	106.2	99.2	165.4	39.6	S	S	S
		4.253 ^a			560 ^a			135 ^a			163 ^a				
		4.218 ^b			591.8 ^b			123.4 ^b			184.7 ^b				
		4.241 ^c			625 ^d			165 ^d			163 ^d				
				507 ^e			96 ^e			163 ^e					
V	4.407	4.095	2.521	328.1	685.8	969.5	213.0	172.8	33.6	42.8	121.5	160.3	S	S	S
		4.127 ^a			660 ^a			174 ^a			118 ^a				
		4.088 ^b			695.9 ^b			146.7 ^b			152.8 ^b				
		4.139 ^c			533 ^d			135 ^d			133 ^d				
Cr	4.302	4.025	2.477	341.1	636.0	894.3	240.2	218.1	102.1	-66.2	7.0	17.0	U	S	S
		4.048 ^b			510.5 ^b			217.2 ^b			6.8 ^b				
Mn	4.229	3.985	2.459	352.0	616.0	898.6	257.6	229.7	98.2	33.5	-10.9	38.3	S	U	S
Fe	4.201	3.968	2.459	356.9	485.9	825.9	258.7	281.4	110.0	112.4	-37.2	29.4	S	U	S
Co	4.221	3.971	2.485	322.5	468.0	542.2	242.9	258.1	191.8	68.2	65.7	17.8	S	S	S
Ni	4.289	4.029	2.520	255.5	434.1	529.5	223.5	212.4	151.0	46.7	87.7	-5.5	S	S	U
Cu	4.398	4.136	2.585	202.7	352.3	356.0	180.0	171.0	160.8	39.4	62.6	7.5	S	S	S
Zn	4.530	4.258	2.674	161.3	288.7	231.5	143.0	139.2	150.7	45.0	67.3	-39.0	S	S	U

a GGA, D. Holec *et al.*, Phys. Rev. B **85**, 064101 (2012).

b Avg. of LDA & GGA, M. G. Brik *et al.*, Comput. Mater. Sci. **51**, 380 (2012).

c Exp., Powder diffraction files: ScN 00-045-0978, TiN 03-065-0565, VN 00-035-0768.

d Exp., J. O. Kim *et al.*, J. Appl. Phys. **72**, 1805 (1992).

e Exp., W. J. Meng *et al.*, Thin Solid Films **271**, 108 (1995).



Comparison of direct *ab initio* results with experimental values

M	a (Å)			C ₁₁ (GPa)			C ₁₂ (GPa)			C ₄₄ (GPa)					
	zb	rs	cc	zb	rs	cc	zb	rs	cc	zb	rs	cc			
Sc	4.883	4.503	2.768	179.6	434.7	502.8	132.9	97.7	42.2	71.8	160.9	-119.2			
		4.44 ^a													
Ti	4.569	4.221	2.607	307.2	657.7	619.6	165.2	121.0	106.2	99.2	165.4	39.6			
		4.241 ^a											625 ^b	165 ^b	163 ^b
													507 ^c	96 ^c	163 ^c
V	4.407	4.095	2.521	328.1	685.8	969.5	213.0	172.8	33.6	42.8	121.5	160.3			
		4.139 ^a											533 ^b	135 ^b	133 ^b

a Powder diffraction files: ScN 00-045-0978, TiN 03-065-0565, VN 00-035-0768.

b J. O. Kim *et al.*, J. Appl. Phys. **72**, 1805 (1992).

c W. J. Meng *et al.*, Thin Solid Films **271**, 108 (1995).



Polycrystalline properties

B (bulk modulus), **G** (shear modulus) and **E** (Young's modulus)

M	B (GPa)			G (GPa)			E (GPa)		
	zb	rs	cc	zb	rs	cc	zb	rs	cc
Sc	148.5	210.0	195.7	45.8	163.9	U	124.7	390.2	U
Ti	212.6	299.9	277.3	86.8	200.9	93.2	229.1	492.8	251.4
V	251.4	343.8	345.6	48.2	164.7	250.5	135.9	426.1	605.2
Cr	273.9	357.4	366.2	U	49.6	98.1	U	142.1	270.3
Mn	289.1	358.5	365.0	38.4	U	121.5	110.4	U	328.1
Fe	291.4	349.5	348.6	80.6	U	103.6	221.5	U	282.8
Co	269.5	328.0	308.6	55.0	79.3	54.2	154.4	220.2	153.7
Ni	234.2	286.3	277.1	30.4	96.3	U	87.5	259.8	U
Cu	187.6	231.5	225.9	24.0	72.6	27.7	69.1	197.3	79.8
Zn	149.1	189.1	177.6	24.1	70.2	U	68.6	187.3	U

zb (zincblende)
rs (rocksalt)
cc (cesium chloride)



Polycrystalline properties

P_C (Cauchy's pressure), ν (Poisson's ratio) and k (Pugh's ratio)

M	P_C (GPa)			ν			k		
	zb	rs	cc	zb	rs	cc	zb	rs	cc
Sc	61.1	-63.3	U	0.36	0.19	U	0.31	0.78	U
Ti	66.0	-44.4	66.6	0.32	0.23	0.35	0.41	0.67	0.34
V	170.2	51.3	-126.7	0.41	0.29	0.21	0.19	0.48	0.72
Cr	U	211.1	85.1	U	0.43	0.38	U	0.14	0.27
Mn	224.1	U	59.9	0.44	U	0.35	0.13	U	0.33
Fe	146.3	U	80.6	0.37	U	0.36	0.28	U	0.30
Co	174.7	192.4	174.1	0.40	0.39	0.42	0.20	0.24	0.18
Ni	176.8	124.7	U	0.44	0.35	U	0.13	0.34	U
Cu	140.6	108.4	153.3	0.44	0.36	0.44	0.13	0.31	0.12
Zn	98.1	72.0	U	0.42	0.33	U	0.16	0.37	U

zb (zincblende)

rs (rocksalt)

cc (cesium chloride)



Polycrystalline properties

H_V (Vicker's hardness) and θ_D (Debye temperature)

M	H_V (GPa)			θ_D (K)		
	zb	rs	cc	zb	rs	cc
Sc	3.6	25.7	U	506.8	901.5	U
Ti	7.8	24.9	6.6	654.9	947.1	648.4
V	2.2	14.8	31.9	473.6	830.9	1002.8
Cr	U	1.5	5.3	U	457.0	630.4
Mn	1.2	U	7.9	403.5	U	681.4
Fe	4.8	U	6.2	573.8	U	626.2
Co	2.6	4.1	2.2	466.8	542.6	448.9
Ni	1.0	6.8	U	352.1	600.1	U
Cu	0.8	5.1	0.9	306.8	511.9	318.3
Zn	1.1	6.0	U	307.6	502.9	U

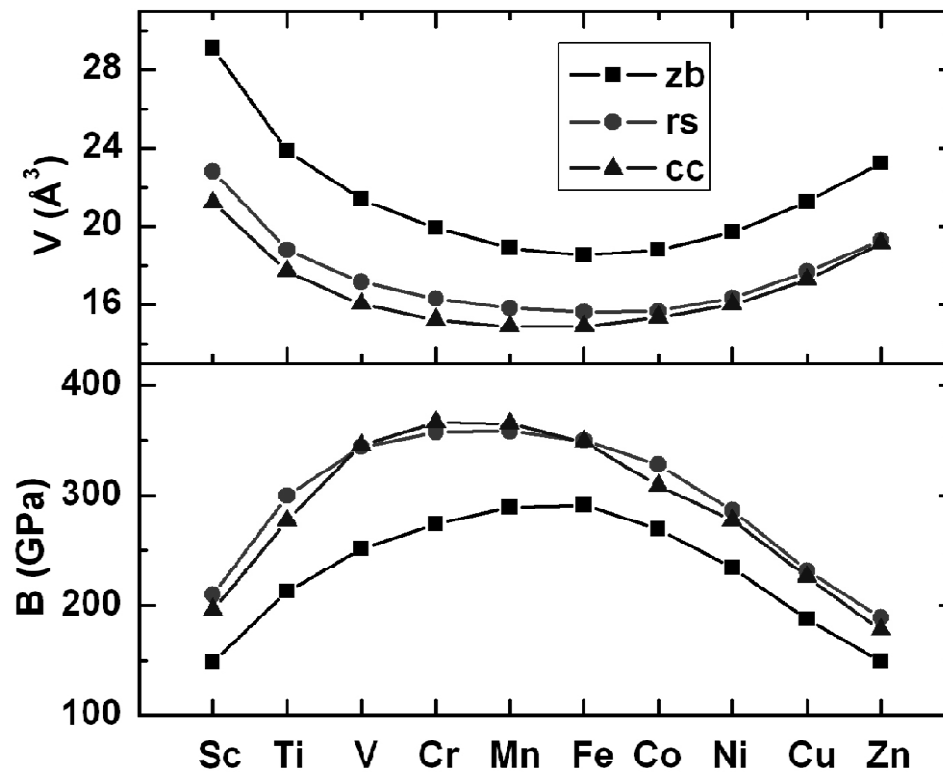
zb (zincblende)

rs (rocksalt)

cc (cesium chloride)



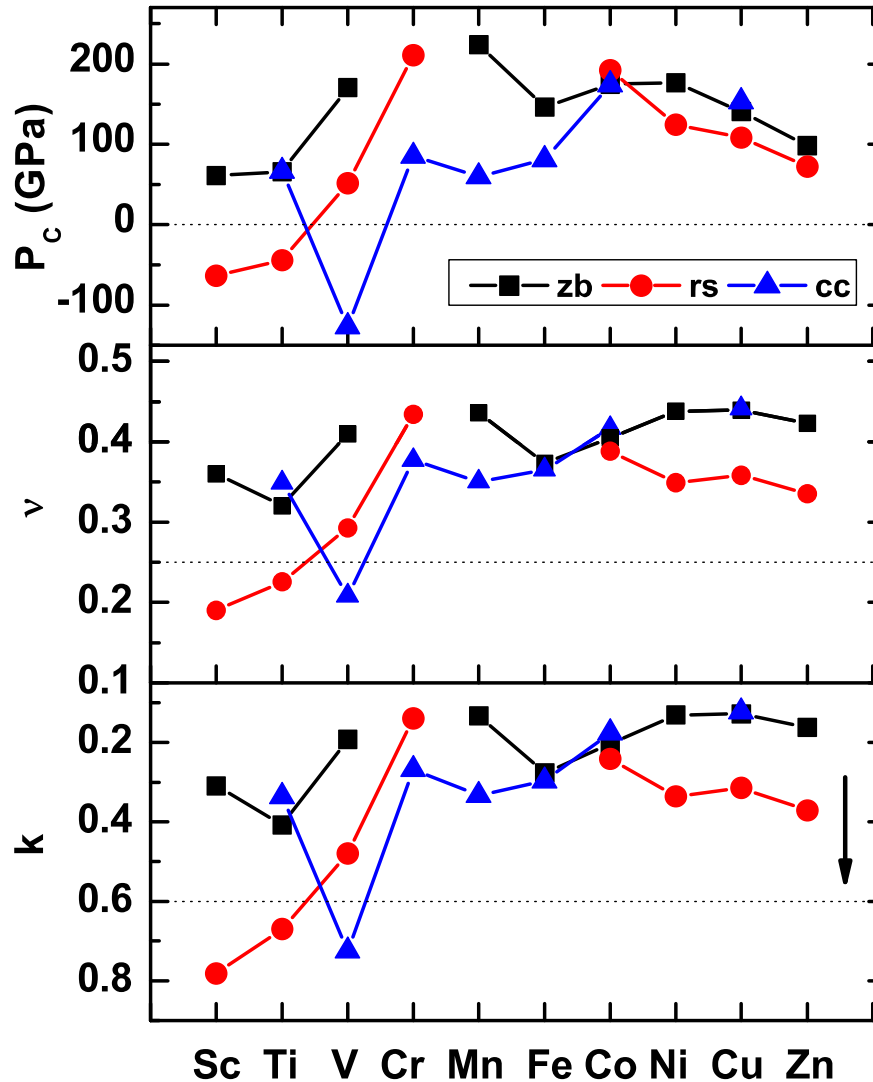
V (unit cell volume) and B (bulk modulus)



$$B = (C_{11} + 2C_{12})/3$$



P_C , ν and k



P_C (Cauchy's pressure)

$$P_C = C_{12} - C_{44}$$

ν (Poisson's ratio)

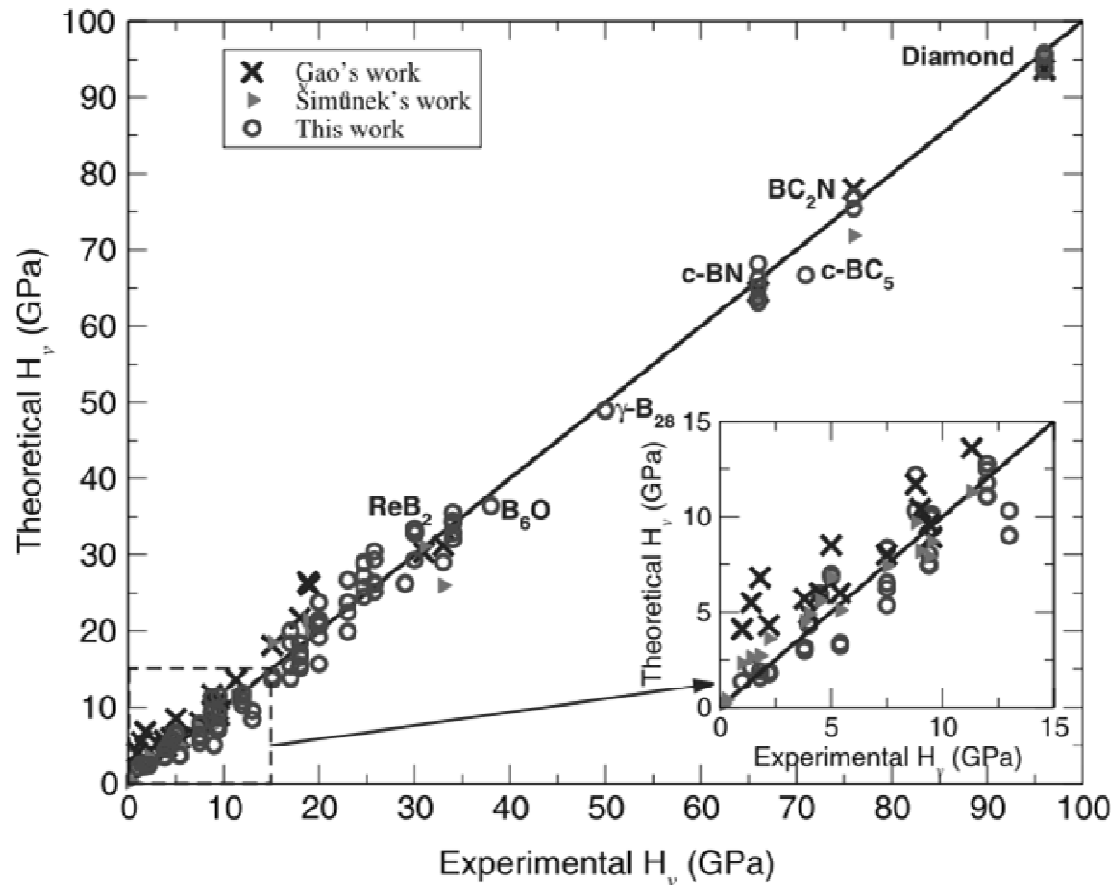
$$\nu = (3B - 2G) / [2(3B + G)]$$

k (Pugh's ratio)

$$k = G/B$$



Chen's formulation for calculating H_V (Vicker's Hardness)



$$B = (C_{11} + 2C_{12})/3$$

$$G_V = [(C_{11} - C_{12}) + 3C_{44}]/5$$

$$G_R = [5(C_{11} - C_{12})C_{44}] / (4C_{44} + 3C_{11} - 3C_{12})$$

$$G = G_{VRH} = (G_V + G_R)/2$$

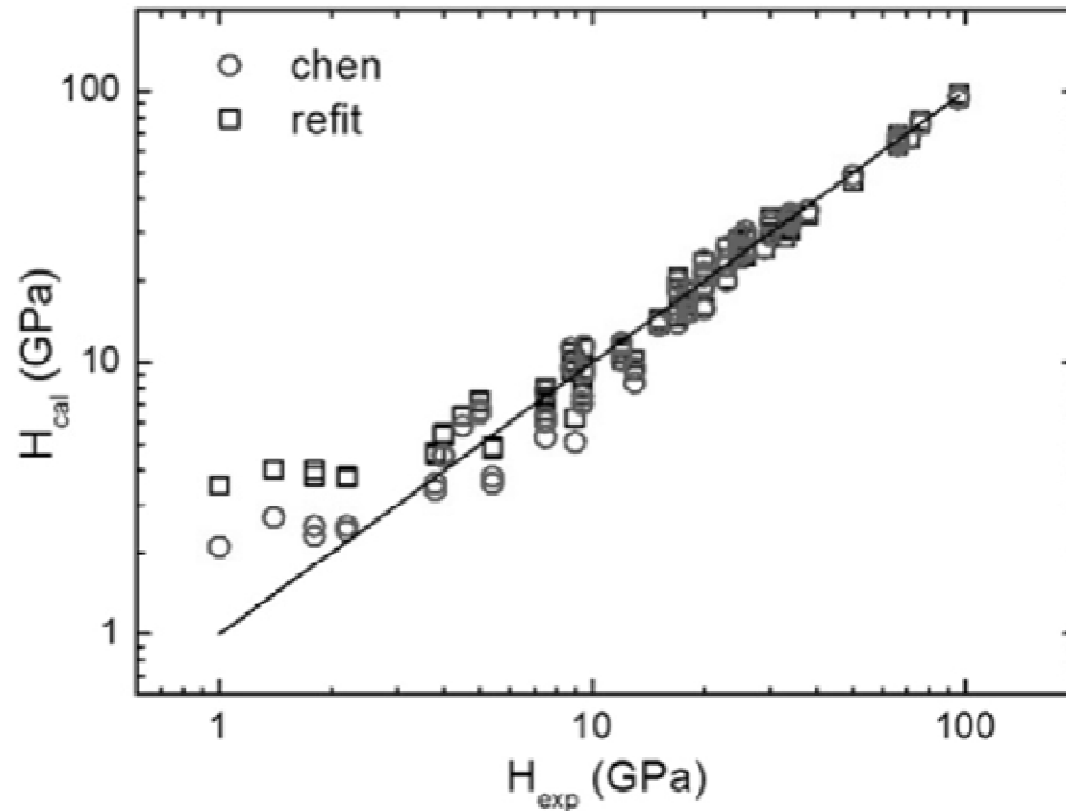
$$k = G/B$$

$$H_V = 2(k^2 G)^{0.585} - 3$$

X. Q. Chen *et al.*, *Intermetallics* **19**, 1275 (2011)



Tian's alternative for calculating H_V (Vicker's Hardness)



$$B = (C_{11} + 2C_{12})/3$$

$$G_V = [(C_{11} - C_{12}) + 3C_{44}]/5$$

$$G_R = [5(C_{11} - C_{12})C_{44}] / (4C_{44} + 3C_{11} - 3C_{12})$$

$$G = G_{VRH} = (G_V + G_R)/2$$

$$k = G/B$$

$$H_V = 0.92k^{1.137} G^{0.708}$$

Y. Tian *et al.*, Int. J. Refract. Met. Hard Mater. **33**, 93 (2012).



Crystal	H_{Exp} (GPa)	H_{Tian} (GPa)	$H_{Simunek}$ (GPa)	H_{Xue} (GPa)	H_{Chen} (GPa)
C	96 ^a	93.6	95.4 ^b	90 ^e	94.6 ^f
Si	12 ^a	13.6	11.3 ^b	14 ^e	11.2 ^f
Ge	8.8 ^b	11.7	9.7 ^b	11.4 ^e	10.4 ^f
SiC	31 ^b	30.3	31.1 ^b	27.8 ^e	33.8 ^f
BN	63 ^a	64.5	63.2 ^b	47.7 ^e	65.3 ^f
BP	33 ^a	31.2	26 ^b	24.9 ^e	29.3 ^f
BAs	19 ^b	26	19.9 ^b	21.1 ^e	–
AlN	18 ^a	21.7	17.6 ^b	14.5 ^e	16.8 ^f
AlP	9.4 ^a	9.6	7.9 ^b	7.4 ^e	7.2 ^f
AlAs	5.0 ^a	8.5	6.8 ^b	6.3 ^e	6.6 ^f
AlSb	4.0 ^a	4	4.9 ^b	4.9 ^e	4.4 ^f
GaN	15.1 ^a	18.1	18.5 ^b	13.5 ^e	13.9 ^f
GaP	9.5 ^a	8.9	8.7 ^b	8 ^e	9.9 ^f
GaAs	7.5 ^a	8	7.4 ^b	7.1 ^e	7.8 ^f
GaSb	4.5 ^a	6	5.6 ^b	4.5 ^e	5.8 ^f
InN	9 ^a	10.4	8.2 ^b	7.4 ^e	7.4 ^f
InP	5.4 ^a	6	5.1 ^b	3.9 ^e	3.7 ^f
InAs	3.8 ^a	3.8	5.7 ^b	4.5 ^e	3.3 ^f
InSb	2.2 ^a	4.3	3.6 ^b	2.2 ^e	2.4 ^f
ZnS	1.8 ^b	6.8	2.7 ^b	2.4 ^e	2.4 ^f
ZnSe	1.4 ^b	5.5	2.6 ^b	1.8 ^e	2.7 ^f
ZnTe	1 ^b	4.1	2.3 ^b	0.9 ^e	2.1 ^f
TiC	32 ^c	34	18.8 ^b	23.9 ^e	27 ^f
TiN	20.6 ^c	21.6	18.7 ^b	23.8 ^h	23.3 ^f
ZrC	25 ^c	21	10.7 ^g	15.7 ^h	27.5 ^f

Y. Tian *et al.*, Int. J. Refract. Met. Hard Mater. **33**, 93 (2012).



Crystal	H_{Exp} (GPa)	H_{Tian} (GPa)	$H_{Simunek}$ (GPa)	H_{Xue} (GPa)	H_{Chen} (GPa)
ZrN	15.8 ^c	16.7	10.8 ^g	15.9 ^h	–
HfC	26.1 ^c	26.8	10.9 ^g	15.6 ^h	–
HfN	16.3 ^c	18	10.6 ^g	15.2 ^h	19.2 ^f
VC	27.2 ^c	23	25.2 ^g	17.5 ^h	26.2 ^f
VN	15.2 ^c	14.9	26.5 ^g	16.5 ^h	–
NbC	17.6 ^c	16.1	18.3 ^b	12.8 ^h	15.4 ^f
NbN	13.7 ^c	13.6	19.5 ^b	12 ^h	14.7 ^f
TaC	24.5 ^c	26	19.9 ^g	14.7 ^h	–
TaN	22 ^c	20	21.2 ^g	14.3 ^h	–
CrN	11 ^c	11	36.6 ^g	19.2 ^h	–
WC	30 ^c	31	21.5 ^b	20.6 ^e	31.3 ^f
Re ₂ C	17.5 ^j	19.7 ^j	11.5 ^g	16.2 ^h	26.4 ⁱ
Al ₂ O ₃	20 ^c	18.8	13.5 ^g	18.4 ^h	20.3 ⁱ
MgO	3.9 ^d	4.5	4.4 ^g	5.4 ^h	24.8 ⁱ
LiF	1 ^d	0.8	2.2 ^g	–	8.5 ⁱ
NaF	0.6 ^d	0.85	1 ^g	–	5.7 ⁱ
NaCl	0.2 ^d	0.4	0.4 ^b	–	2.4 ⁱ
KCl	0.13 ^d	0.18	0.2 ^b	–	2.3 ⁱ
KBr	0.1 ^d	0.23	0.2 ^g	–	0.1 ⁱ

^a Reference [34].

^b Reference [37].

^c Reference [32].

^d Reference [60].

^e Reference [58].

^f Reference [30].

^g Calculated by authors using method [36].

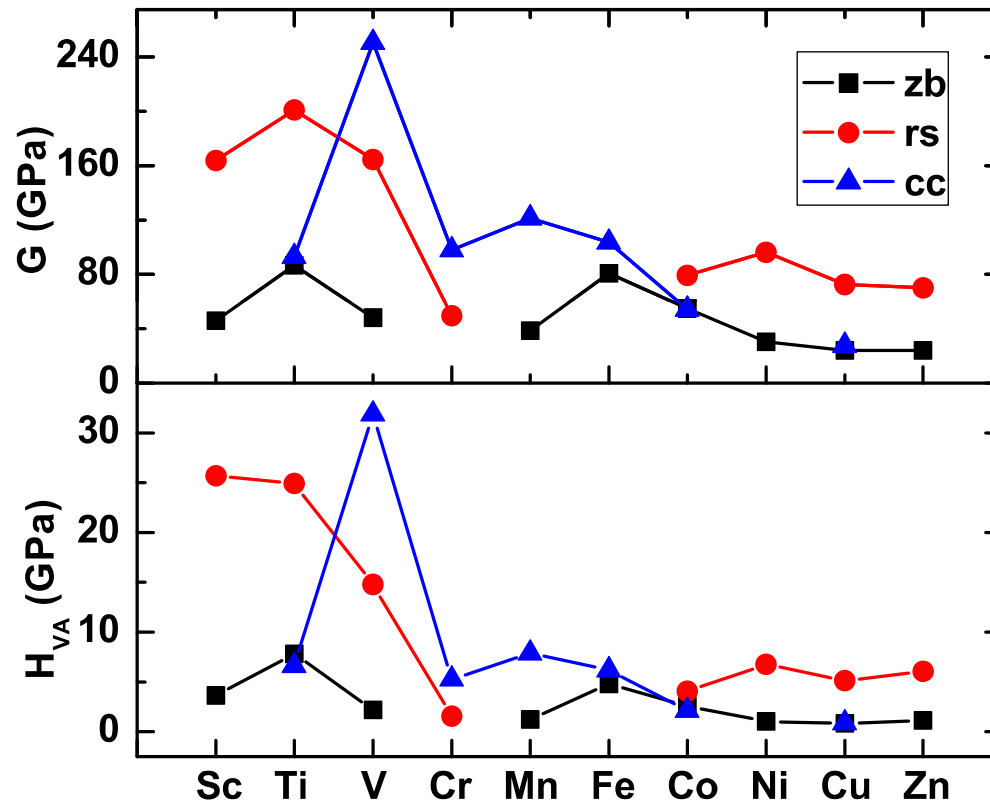
^h Calculated using [35].

ⁱ Calculated with [30].

^j Reference [52].



G (shear modulus) and H_{VA} (Tian's)



$$G_V = [(C_{11} - C_{12}) + 3C_{44}]/5$$

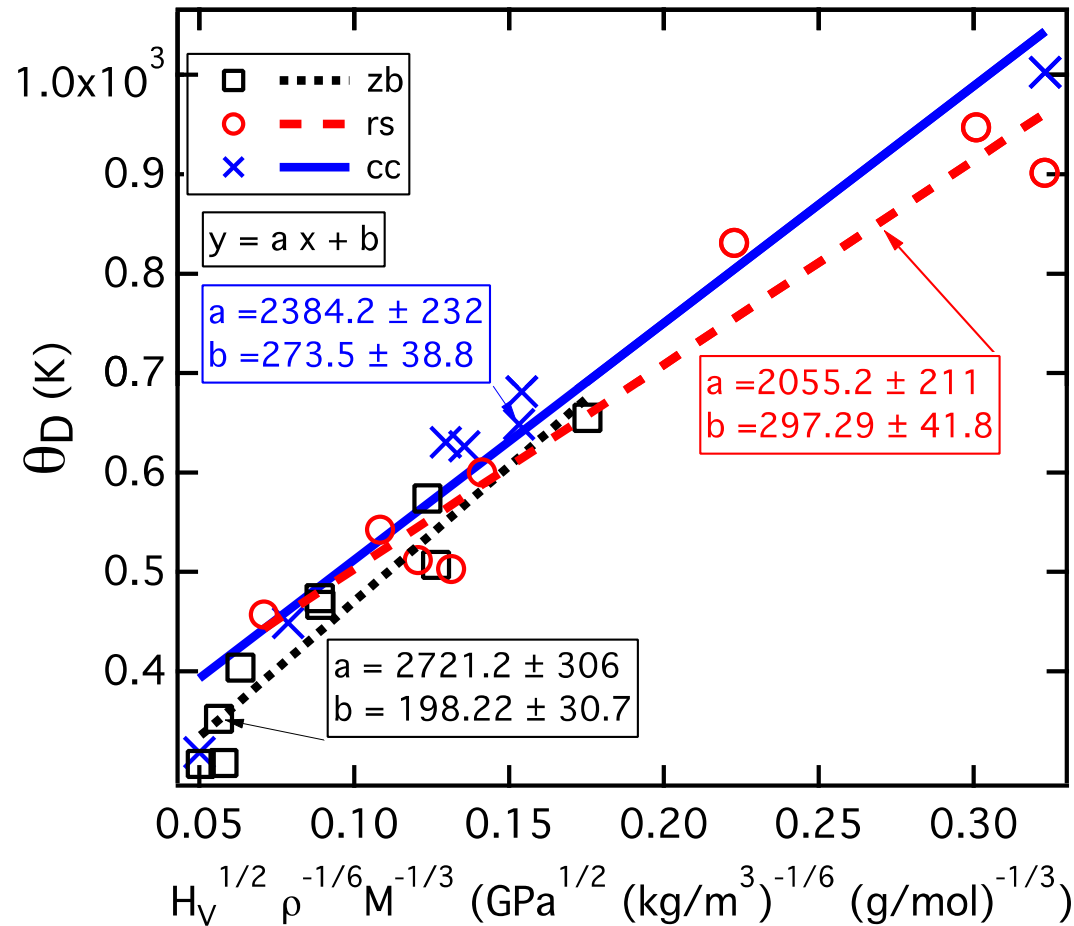
$$G_R = [5(C_{11} - C_{12})C_{44}] / (4C_{44} + 3C_{11} - 3C_{12})$$

$$G = G_{VRH} = (G_V + G_R)/2$$

$$H_{VA} = 0.92 k^{1.137} G^{0.708}$$



θ_D (Debye temperature) vs $f(H_{VA})$



$$\theta_D = \frac{h}{k_B} \left[\frac{3n}{4\pi} \left(\frac{N_A \rho}{M} \right) \right]^{1/3} v_m$$

where $v_m = \left[\frac{1}{3} \left(\frac{2}{v_t^3} + \frac{1}{v_l^3} \right) \right]^{-1/3}$

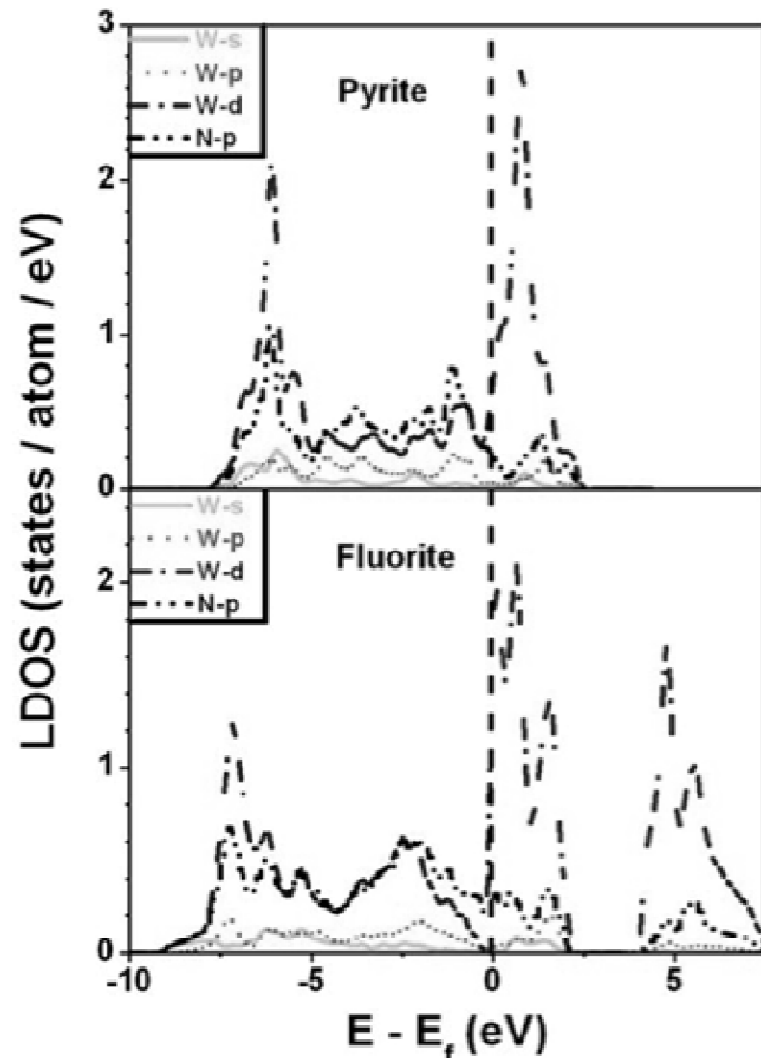
$$v_t = \left(\frac{G}{\rho} \right)^{1/2} \text{ and } v_l = \left(\frac{3B+4G}{3\rho} \right)^{1/2}$$

$$H_{VA} = 0.92 k^{1.137} G^{0.708}$$

P. Deus *et al.*, *Cryst. Res. Technol.* **18**, 491 (1983).



Correlation of stability with DOS

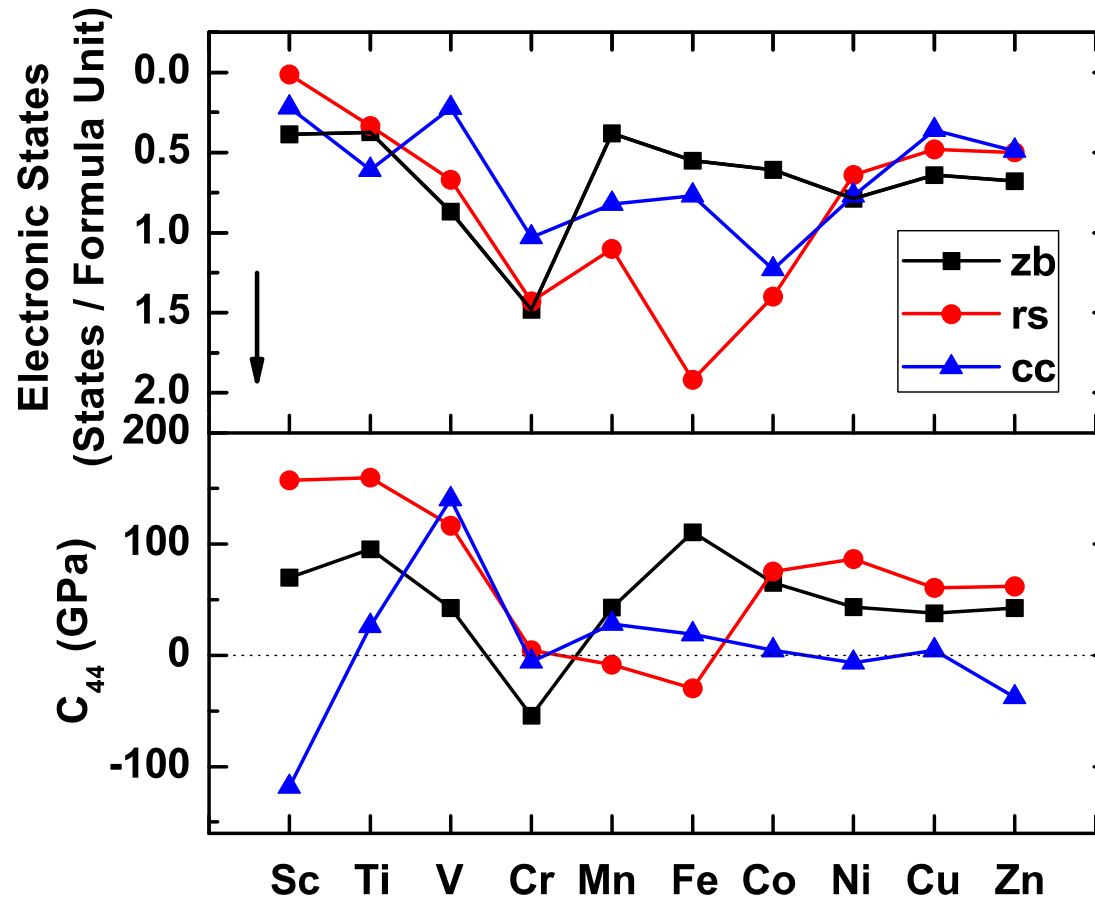


- Pyrite-structured WN_2 is stable, and DOS at E_f is small
- Fluorite-structured WN_2 is unstable, and DOS at E_f is large

S. K. R. Patil *et al.*, Thin Solid Films **517**, 824 (2008)

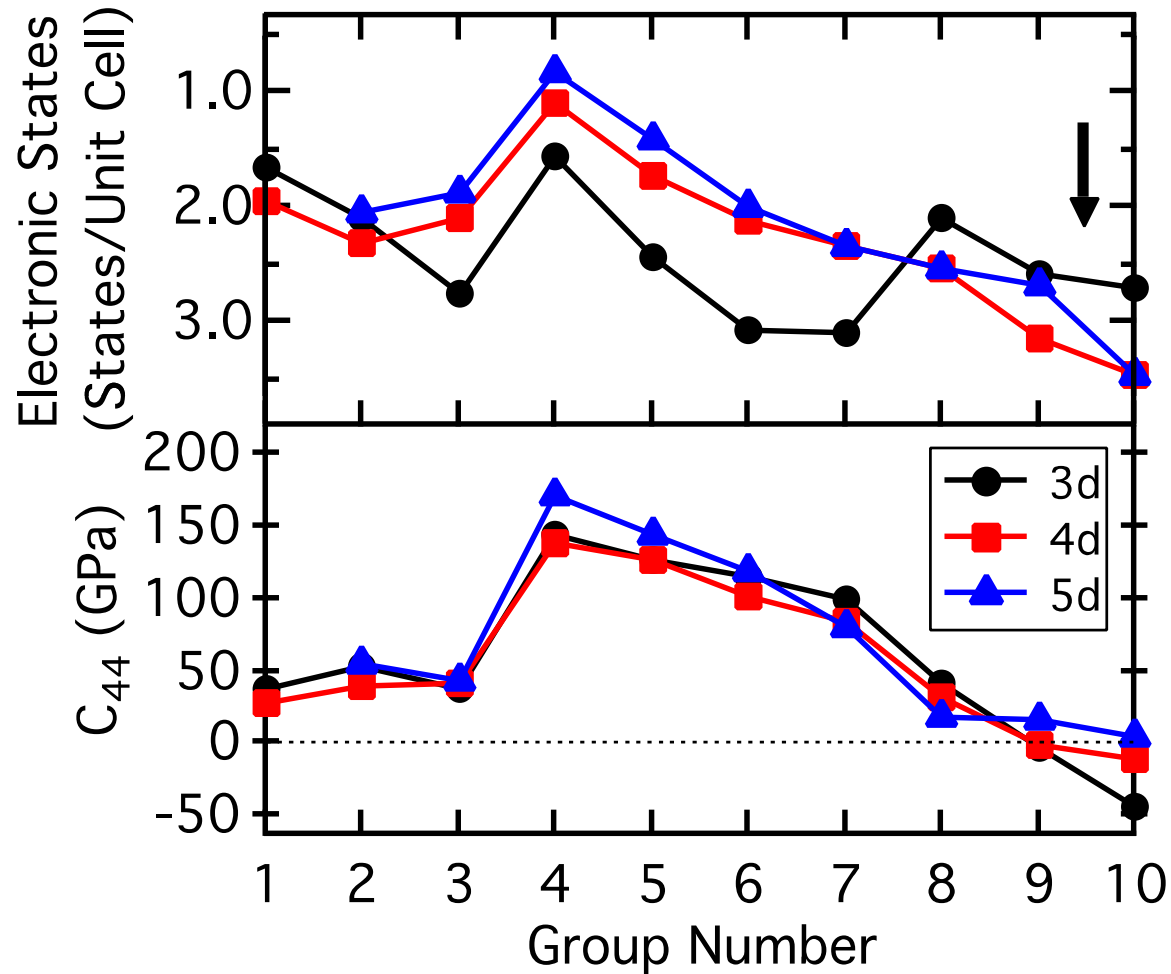


Correlation of C_{44} (indicating H_V and stability) with TDOS



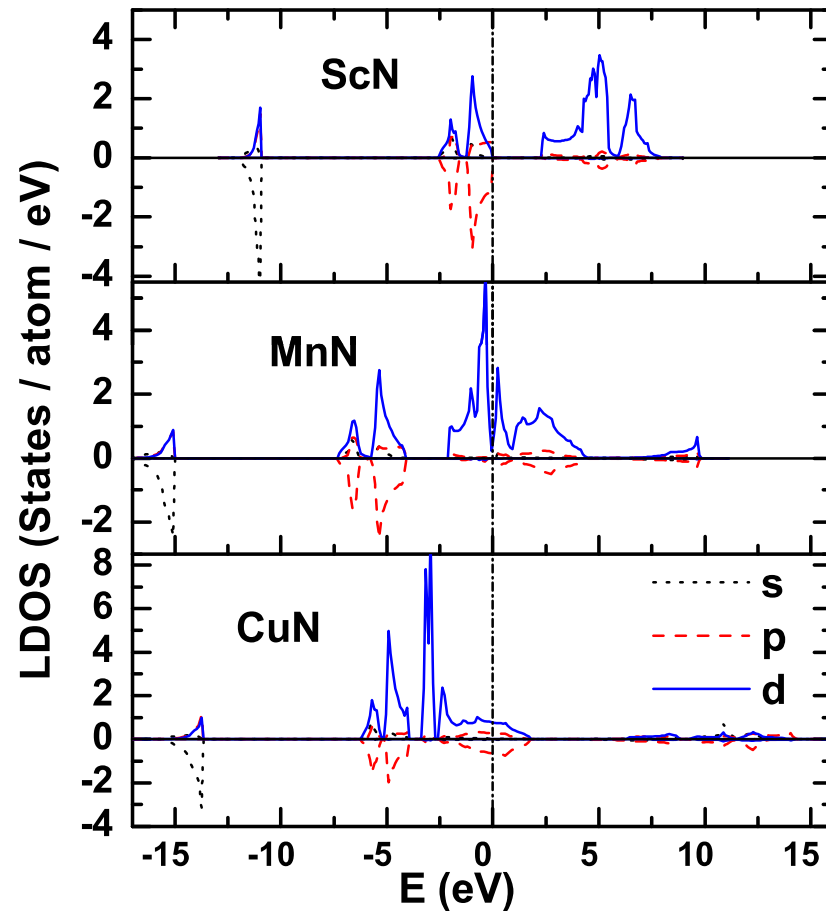


Correlation of C_{44} (indicating H_V and stability) with TDOS of NbO-type





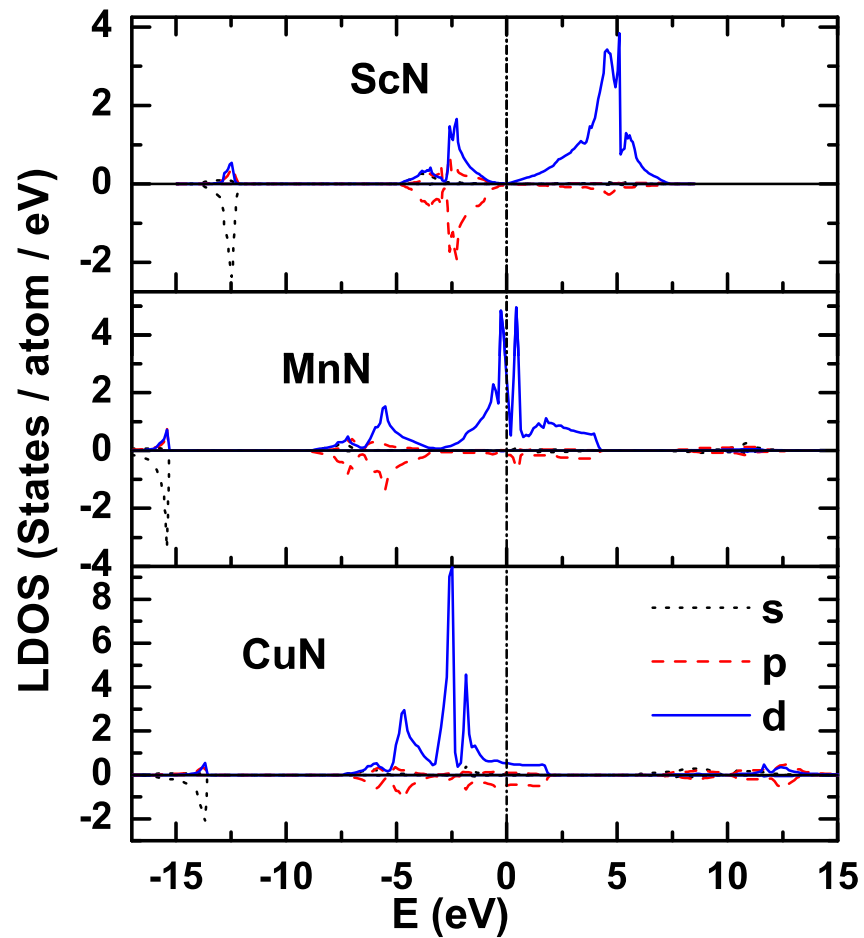
LDOS - zincblende



As transition metal goes from left to right in the 3d row, more states shift below E_F , peaks becoming sharper.



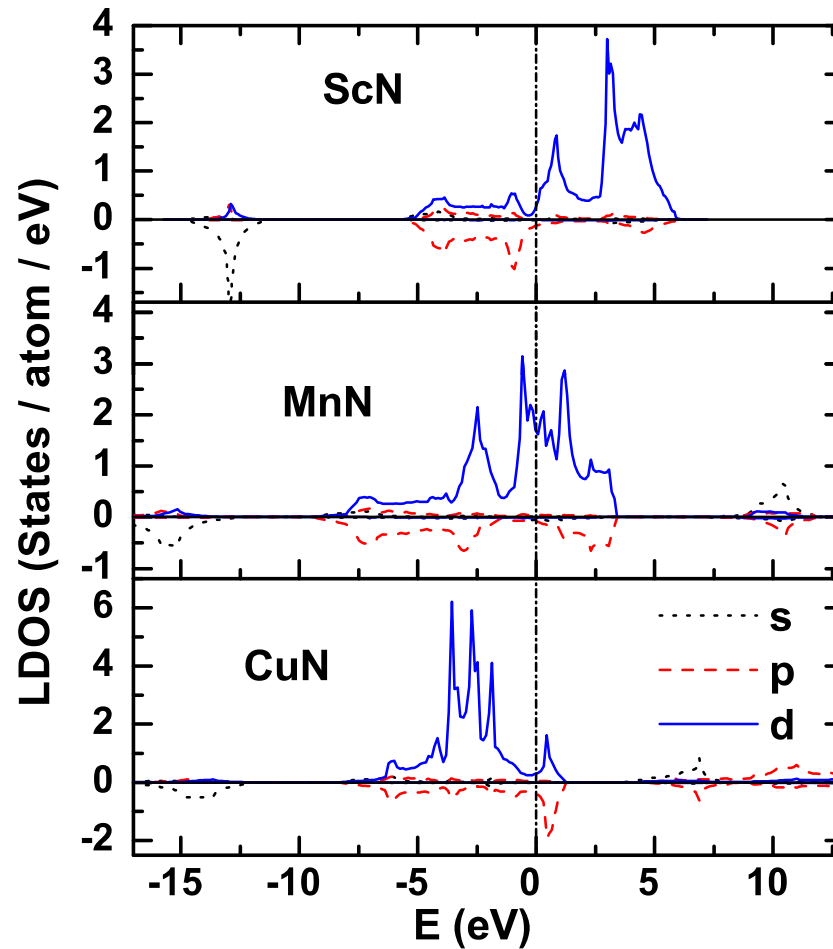
LDOS - rocksalt



As transition metal goes from left to right in the 3d row, more states shift below E_F , peaks becoming sharper.



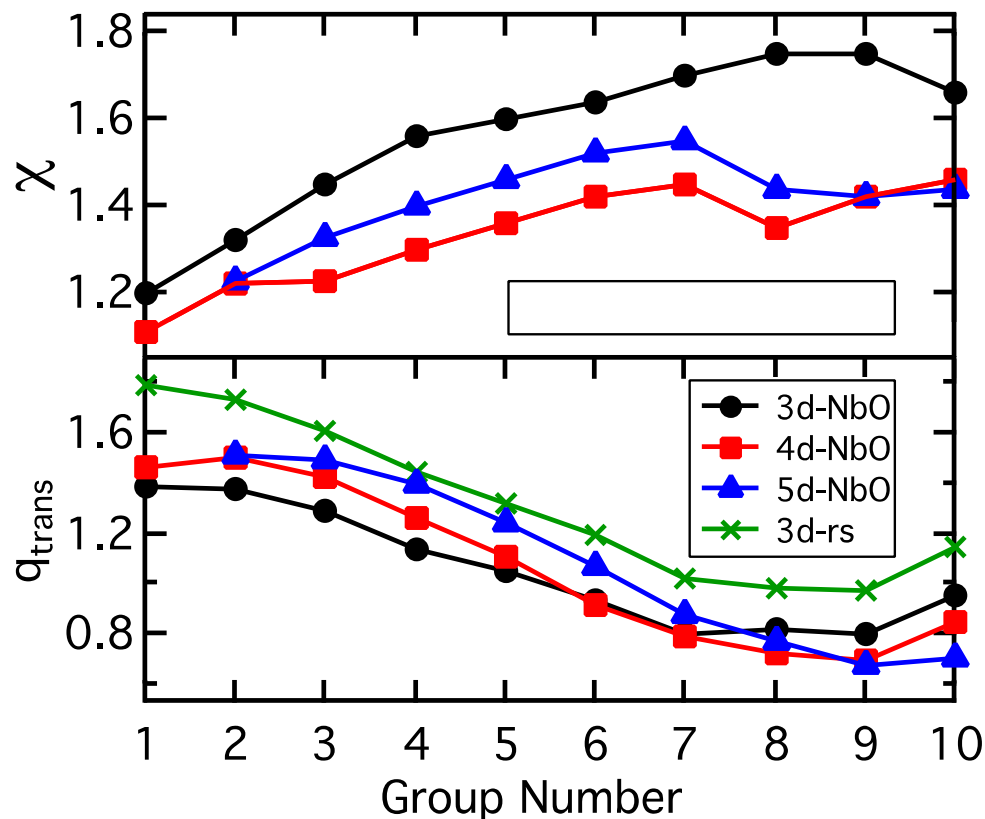
LDOS – cesium chloride



As transition metal goes from left to right in the 3d row, more states shift below E_F , peaks becoming sharper.



Bader analysis of NbO-type



χ (nitrogen): 3.07

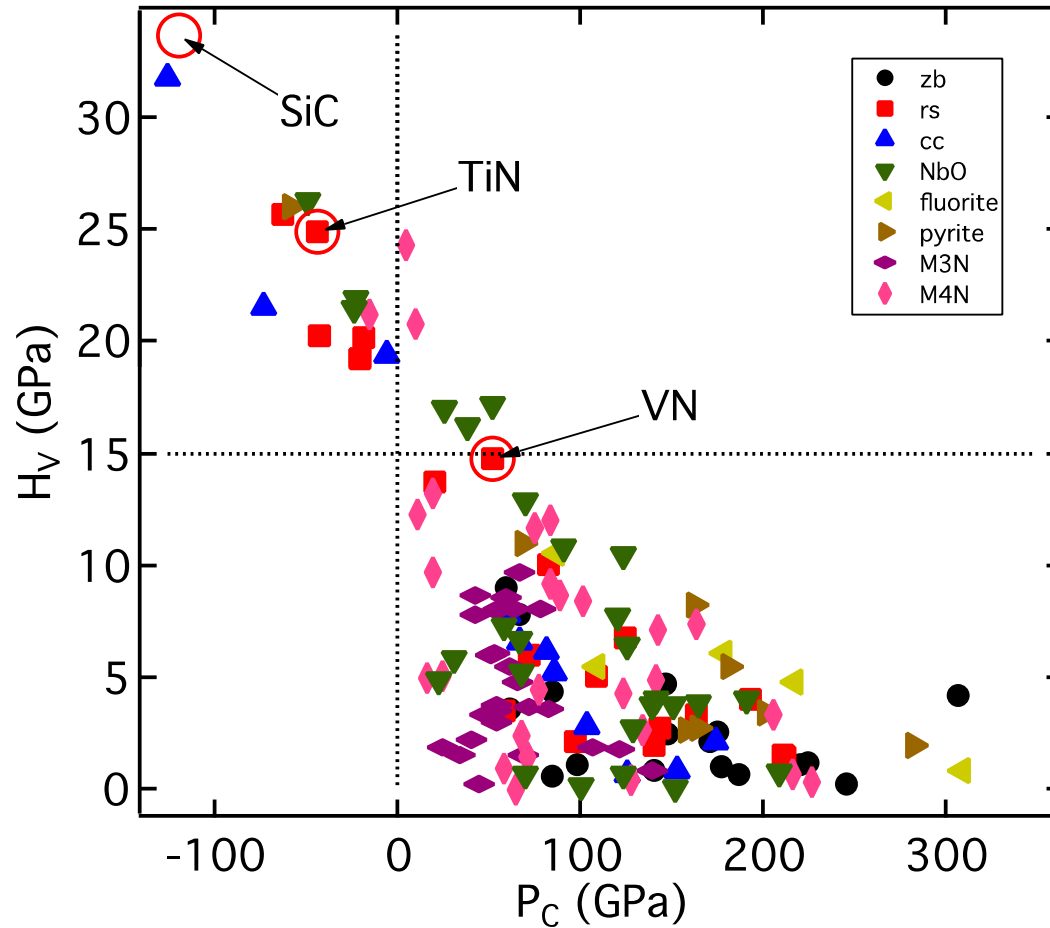
χ (electronegativity) from
A. L. Allred *et al.*, J. Inorg. Nucl.
Chem. **5**, 264 (1958).

q_{trans} (charge transfer from
transition metal to nitrogen using
Bader's scheme)

Bader analysis program from
W. Tang *et al.*, J. Phys.: Condens. Matter **21**,
084204 (2009)
E. Sanville *et al.*, J. Comp. Chem. **28**, 899-908
(2007)
G. Henkelman *et al.*, Comput. Mater. Sci. **36**, 254-
360 (2006)



H_{VA} vs P_C (Cauchy's pressure)



Data partly from

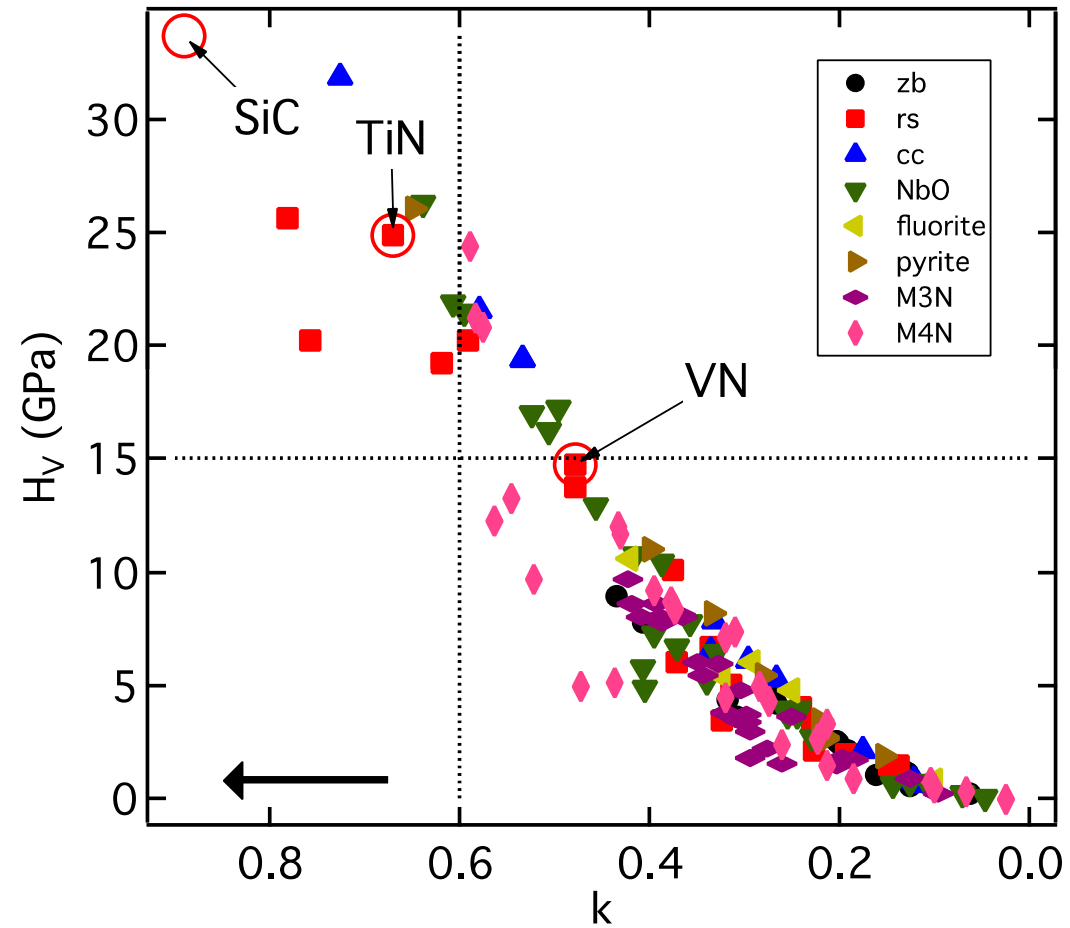
W. Chen *et al.*, *J. Alloys Compd.* **499**, 243 (2010).

E. J. Zhao *et al.*, *Comput. Mater. Sci.* **47**, 1064 (2010).

E. J. Zhao *et al.*, *J. Solid State Chem.* **181**, 2814 (2008).

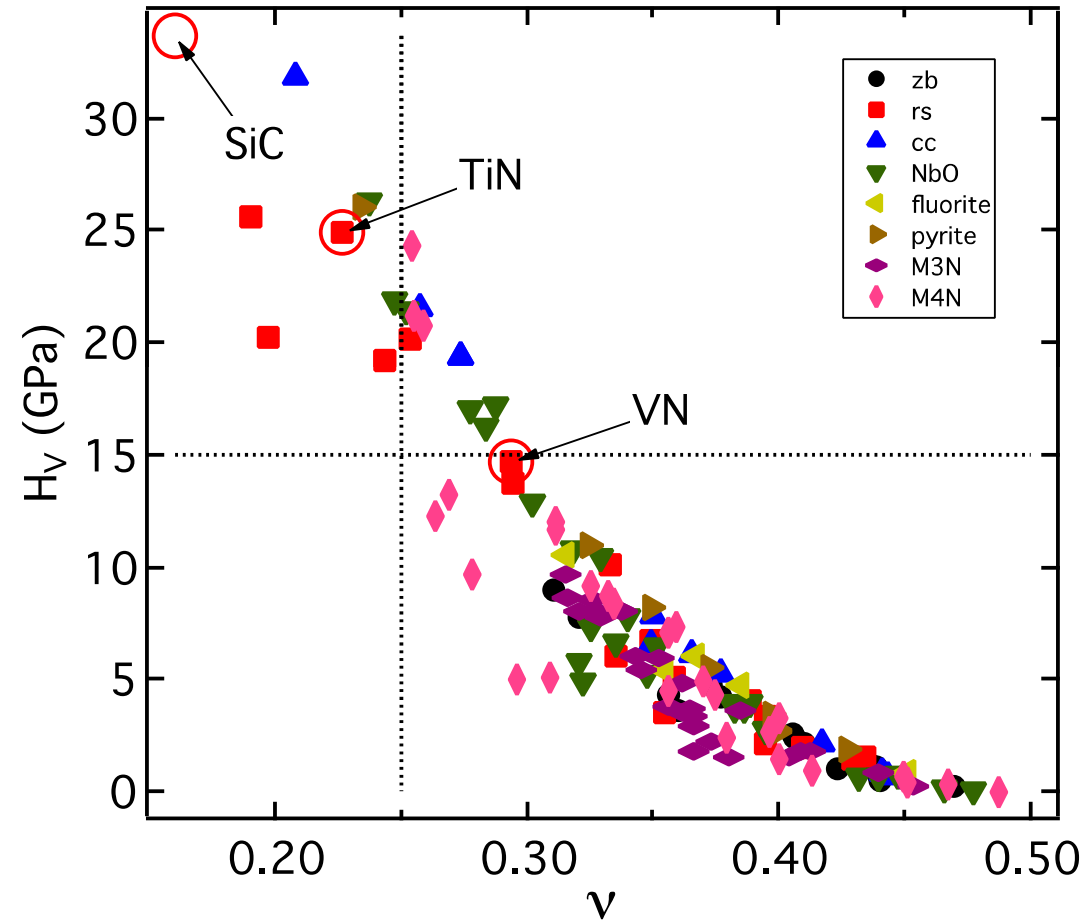


H_{VA} vs k (Pugh's ratio) x-axis inverted



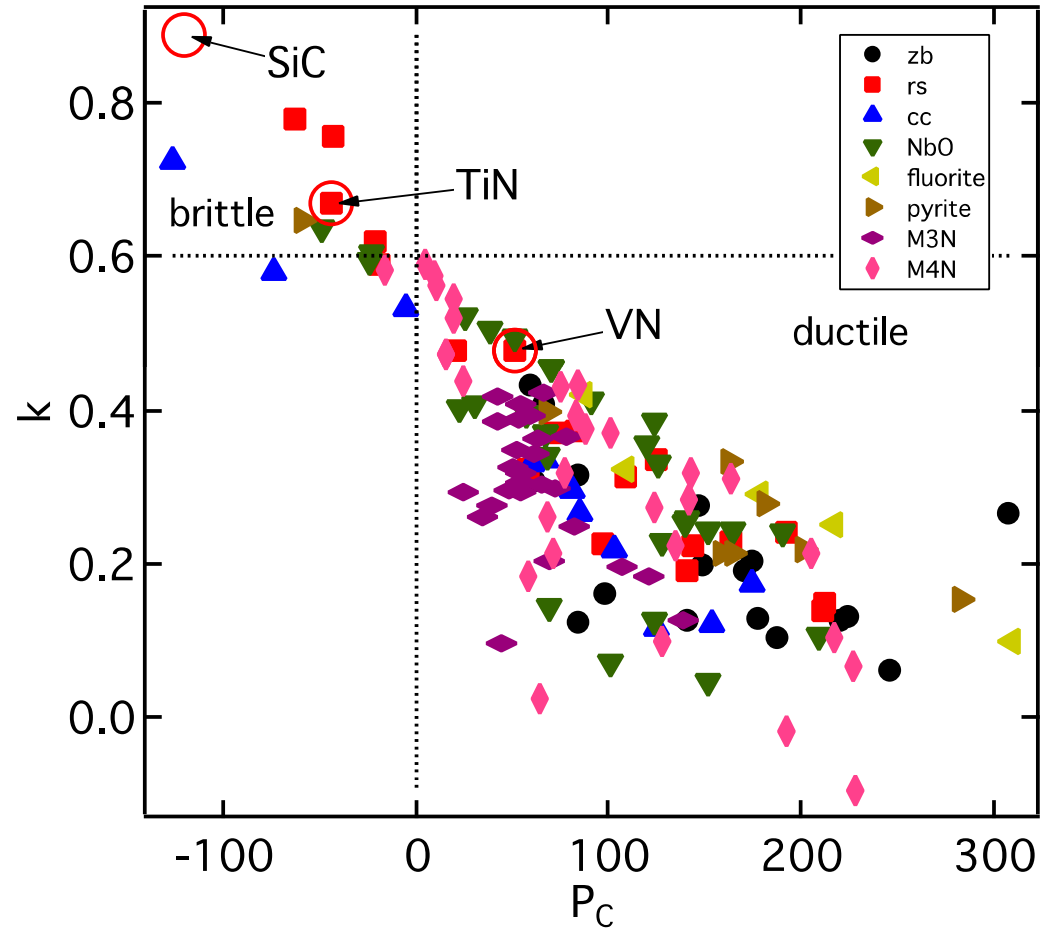


H_{VA} vs ν (Poisson's ratio)





k vs P_c





Nitrides with $H_{VA} \geq 15$ GPa

Material	a (Å)	C ₁₁	C ₁₂	C ₄₄	B (GPa)	G (GPa)	ν	k	P _c (GPa)	H _{VA} (GPa)
diamond	3.548	1079.8	131.4	577.2	447.5	533.5	0.07	1.19	-445.80	95.80
SiC	4.345	396.5	128.5	249.2	217.8	194.3	0.16	0.89	-120.70	33.70
M ₄ N-Mn ₄ N	3.653	769.2	127.6	143.8	341.4	199.5	0.26	0.58	-16.20	21.23
M ₄ N-Tc ₄ N	3.971	670.3	184.1	174.3	346.1	199.2	0.26	0.58	9.81	20.83
M ₄ N-Re ₄ N	3.993	772.4	221.1	217.0	404.8	238.8	0.25	0.59	4.06	24.37
rs-ScN	4.503	434.7	97.7	160.9	210.0	163.9	0.19	0.78	-63.27	25.67
rs-TiN	4.221	657.7	121.0	165.4	299.9	200.9	0.23	0.67	-44.40	24.93
rs-VN	4.095	685.8	172.8	121.5	343.8	164.7	0.29	0.48	51.32	14.78
rs-YN	4.890	319.0	84.0	127.0	162.3	123.1	0.20	0.76	-43.00	20.28
rs-ZrN	4.580	563.0	101.0	122.0	255.0	158.0	0.24	0.62	-21.00	19.23
rs-HfN	4.436	704.9	111.8	131.0	309.5	182.9	0.25	0.59	-19.20	20.22
cc-VN	2.521	969.5	33.6	160.3	345.6	250.5	0.21	0.72	-126.72	31.85
cc-TaN	2.731	1006.0	33.0	107.0	357.3	207.2	0.26	0.58	-74.00	21.60
cc-ReN	2.679	900.0	122.0	128.0	381.3	203.7	0.27	0.53	-6.00	19.45
NbO-CrN	3.802	724.9	123.2	146.9	323.8	196.6	0.25	0.61	-23.72	21.94
NbO-MnN	3.744	683.9	156.9	131.4	332.6	174.3	0.28	0.52	25.55	17.04
NbO-MoN	4.096	763.6	115.3	139.6	331.4	197.1	0.25	0.59	-24.28	21.47
NbO-TcN	4.030	686.0	169.6	131.6	341.7	173.0	0.28	0.51	37.94	16.30
NbO-WN	4.092	857.9	123.1	172.5	368.1	234.7	0.24	0.64	-49.36	26.30
NbO-ReN	4.041	761.0	200.9	149.5	387.6	192.7	0.29	0.50	51.37	17.24
pyrite-PtN ₂	4.792	845.0	101.0	160.0	349.0	226.0	0.23	0.65	-59.00	26.06



Database



Cubic forms of 3d, 4d and 5d transition metal nitrides in M:N ratios from 4:1 to 1:1 to 1:3. Dark green regions have completed *ab initio* results!

Structures	Formula	Stoichiometry	3d	4d	5d
M ₄ N	M ₄ N	4:1	Dark Green	Dark Green	Dark Green
Anti-ReO ₃	M ₃ N	3:1	Dark Green	Dark Green	Dark Green
Zincblende	MN	1:1	Dark Green	Dark Green	Dark Green
Rocksalt	MN	1:1	Dark Green	Dark Green	Dark Green
Cesium chloride	MN	1:1	Dark Green	White	Dark Green
NbO	MN	1:1	Dark Green	Dark Green	Dark Green
Spinel	M ₃ N ₄	0.75:1	White	White	White
Fluorite	MN ₂	0.5:1	White	White	Dark Green
Pyrite	MN ₂	0.5:1	White	White	Dark Green
Skutterudite	MN ₃	0.33:1	White	White	White



Summary



- Computed single crystal V , C_{11} , C_{12} , C_{44} , LDOS and band structures
- Multi-crystal average of B , G , E , ν , k , H_V , θ_D , T_m .
- Showed correlations of hardness and ductility
- Importance of spread out bands and bonding between M-p orbitals and N-d orbitals
- Inverse correlation of DOS at E_F and C_{44} or stability



Future

- Create Web database of 10 cubic binary nitride phases
- Some search ability will exist
- Hexagonal structures
- Ternaries



Hexagonal structures

- Apart from the cubic phases, there are also **experimental** studies of hexagonal structures.
 - AlN, I. W. Kim *et al.*, Appl. Phys. Lett. **78**, 892, (2001)
 - IrN₂, A. F. Young *et al.*, Phys. Rev. Lett. **96**, 155501, (2006)
 - ReN₂, F. Kawamura *et al.*, Appl. Phys. Lett. **100**, 251910, (2012)
 - Re₃N, A. Friedrich *et al.*, Phys. Rev. B **82**, 224106, (2010)



Ternary systems

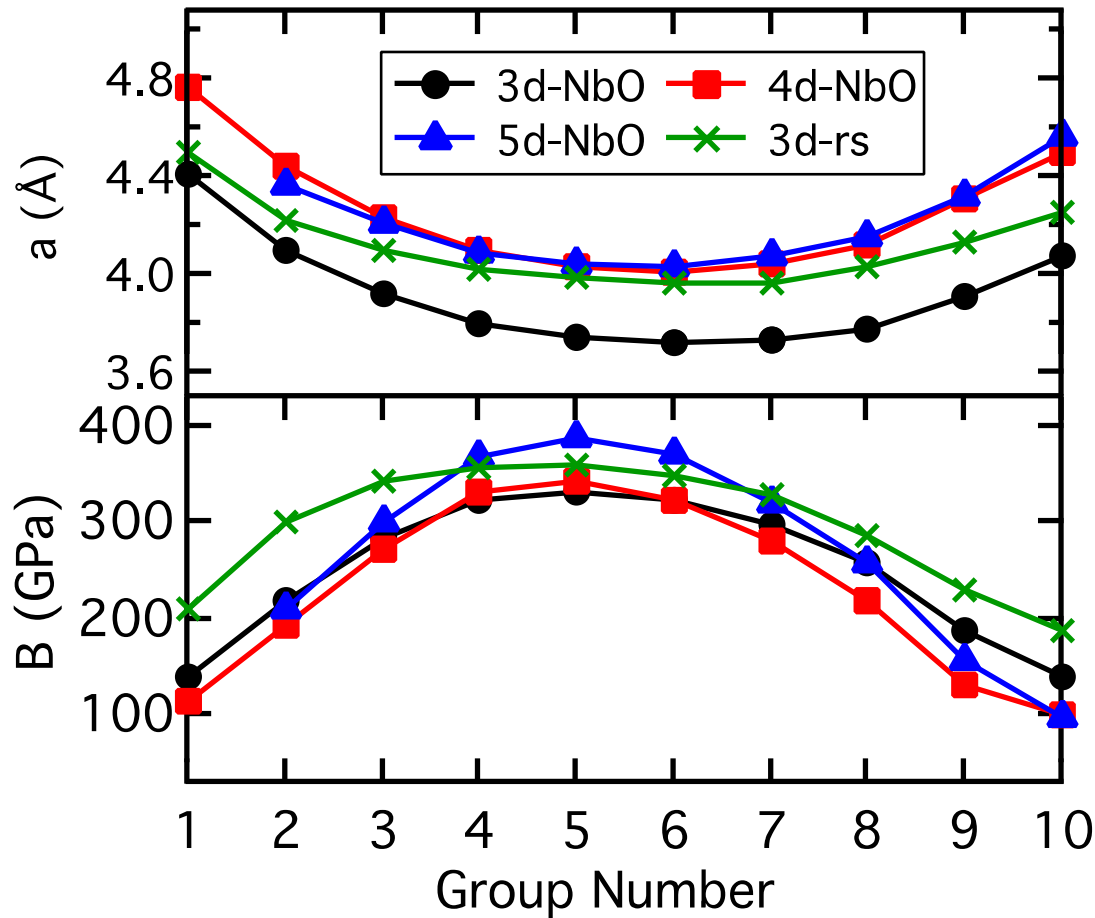
- TM-TM-N:
 - Ti-V-N, Ti-Nb-N, Ti-Mo-N, Ti-W-N, Ti-Ta-N, V-W-N, V-Mo-N, V-Ta-N, D. G. Sangiovanni *et al.*, *Acta Mater.* **59**, 2121, (2011).
- TM-non-TM-N:
 - Ti-Al-N, P. H. Mayrhofer *et al.*, *Appl. Phys. Lett.* **83**, 2049, (2003).



Thank you!



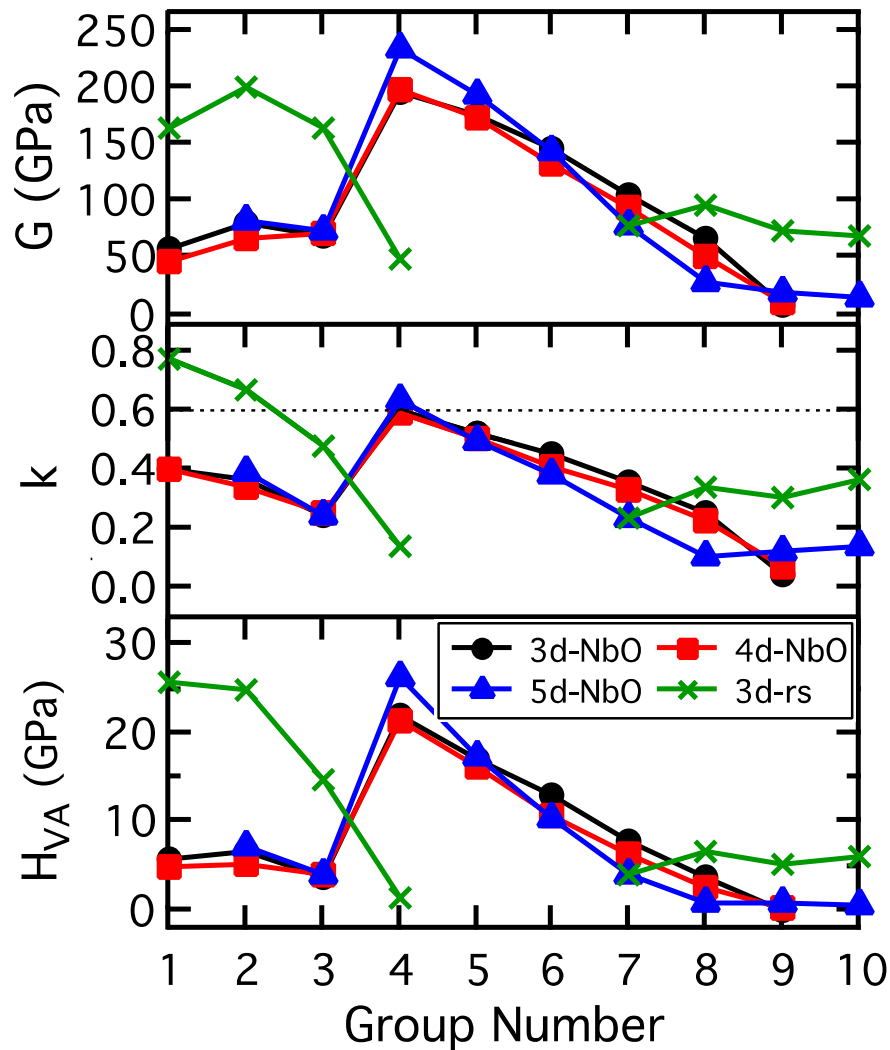
a (lattice constant) and B (bulk modulus)



$$B = (C_{11} + 2C_{12})/3$$



G , k and H_{VA}



G (Shear modulus)

$$G_V = [(C_{11} - C_{12}) + 3C_{44}]/5$$

$$G_R = [5(C_{11} - C_{12})C_{44}] / (4C_{44} + 3C_{11} - 3C_{12})$$

$$G = G_{VRH} = (G_V + G_R)/2$$

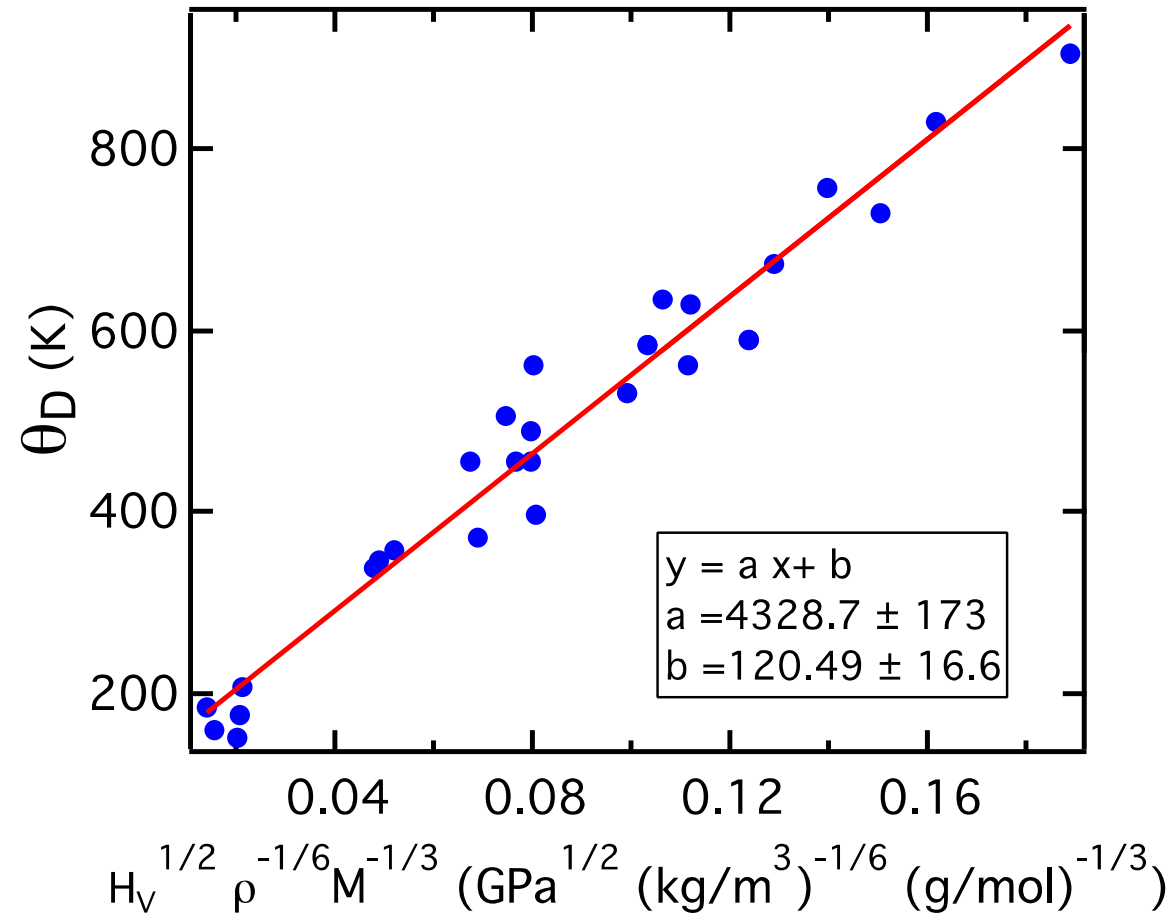
k (Pugh's ratio)

$$k = G/B$$

$$H_{VA} = 0.92 k^{1.137} G^{0.708}$$

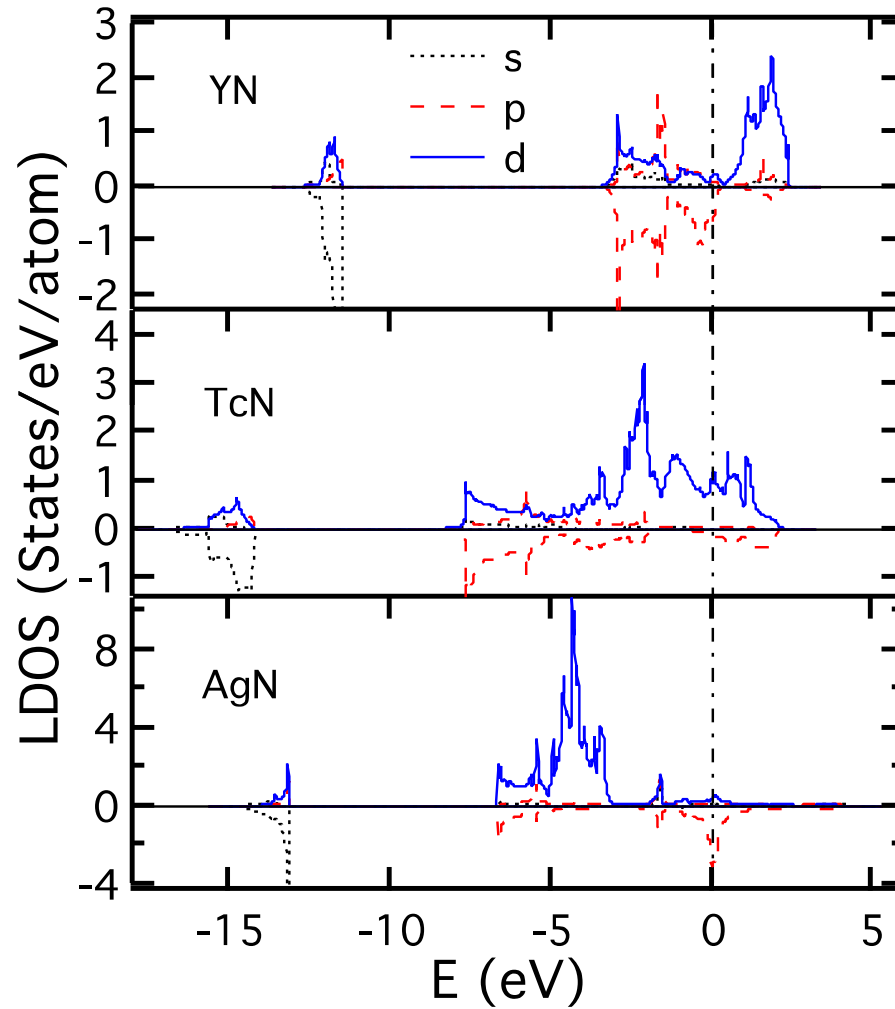


θ_D (Debye temperature) vs $f(H_{VA})$





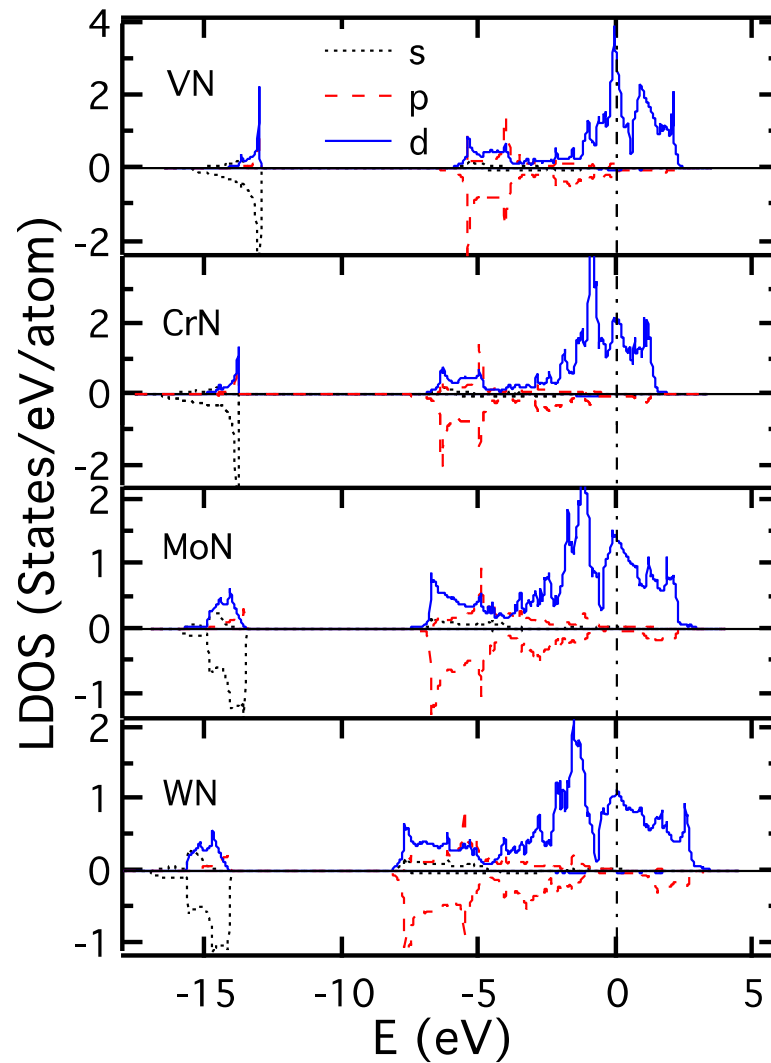
LDOS



As transition metal goes from left to right in the 4d row, more states shift below E_F , peaks becoming sharper.



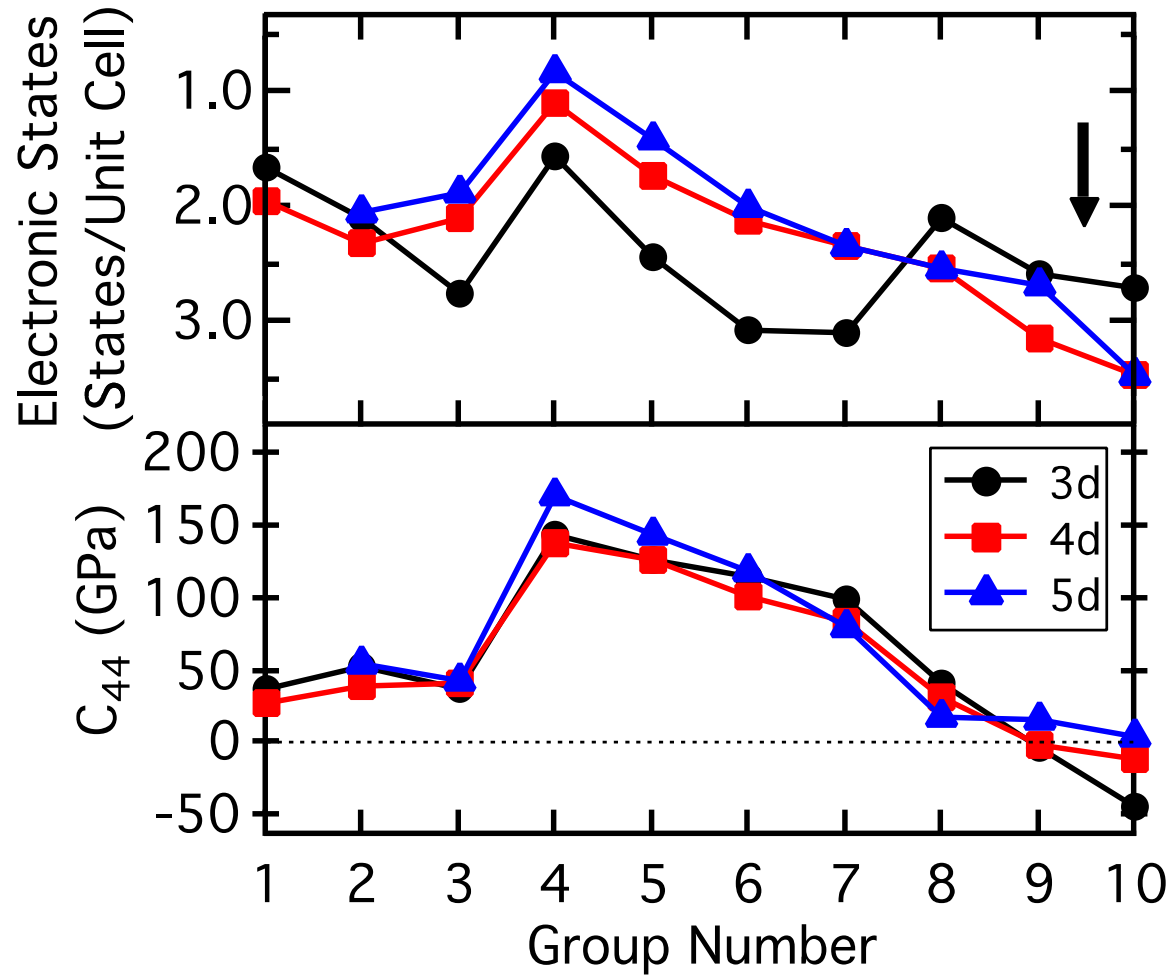
LDOS



As transition metal goes from top to bottom in the group 4 column, almost nothing evident changes.

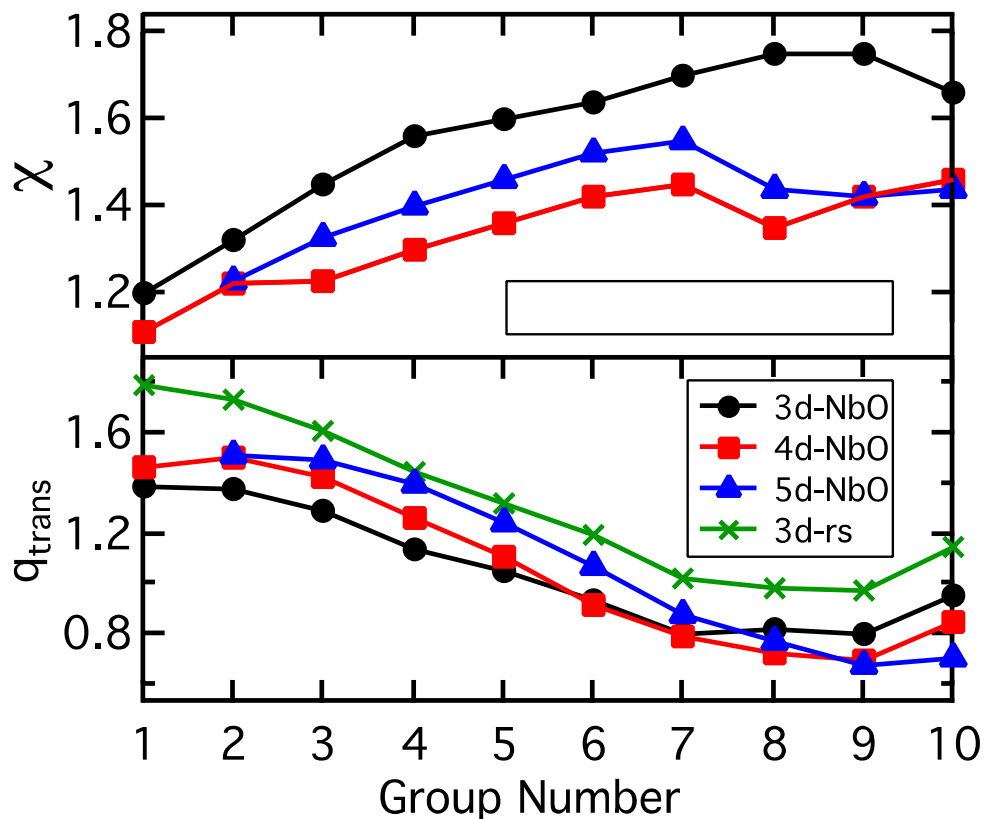


Correlation of C_{44} (indicating H_V and stability) with TDOS





Bader analysis



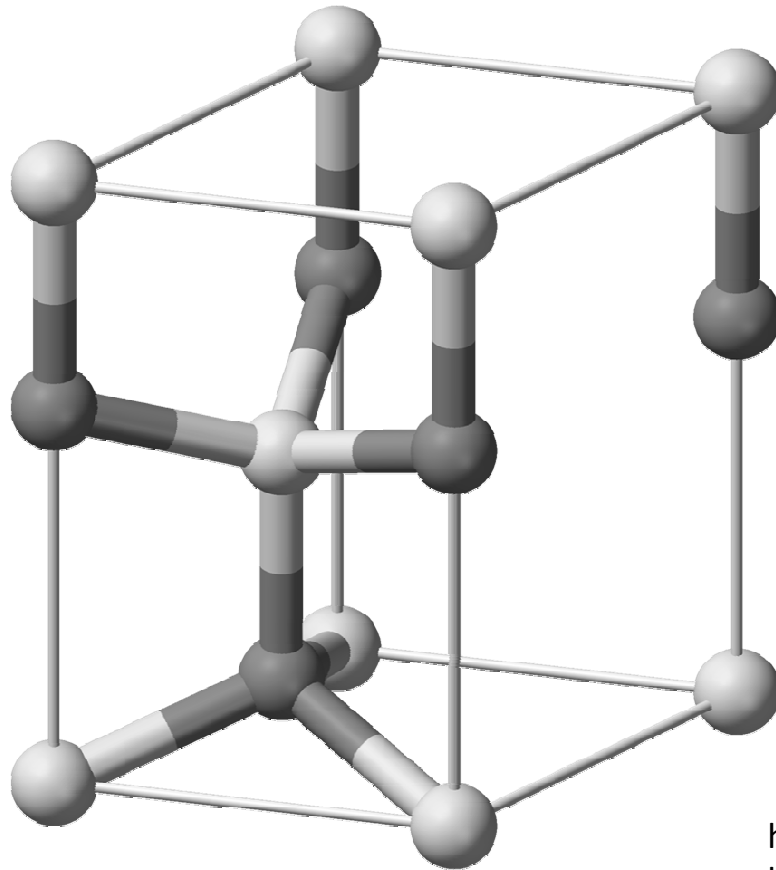
χ (electronegativity)
 q_{trans} (charge transfer from transition metal to nitrogen using Bader's scheme)

W. Tang *et al.*, J. Phys.: Condens. Matter 21, 084204 (2009)
E. Sanville *et al.*, J. Comp. Chem. 28, 899-908 (2007)
G. Henkelman *et al.*, Comput. Mater. Sci. 36, 254-360 (2006)



Hexagonal structures

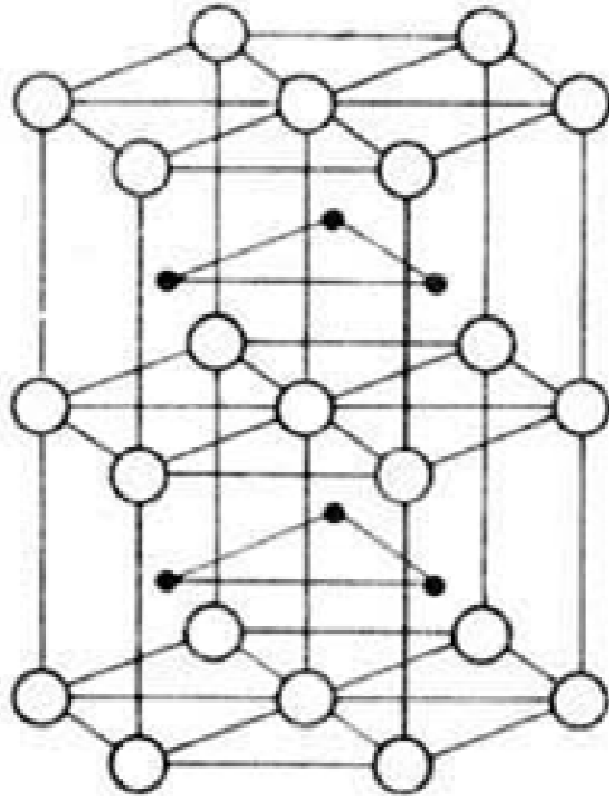
Structure - wurtzite (MN)



<http://en.wikipedia.org/wiki/File:Wurtzite-unit-cell-3D-balls.png>



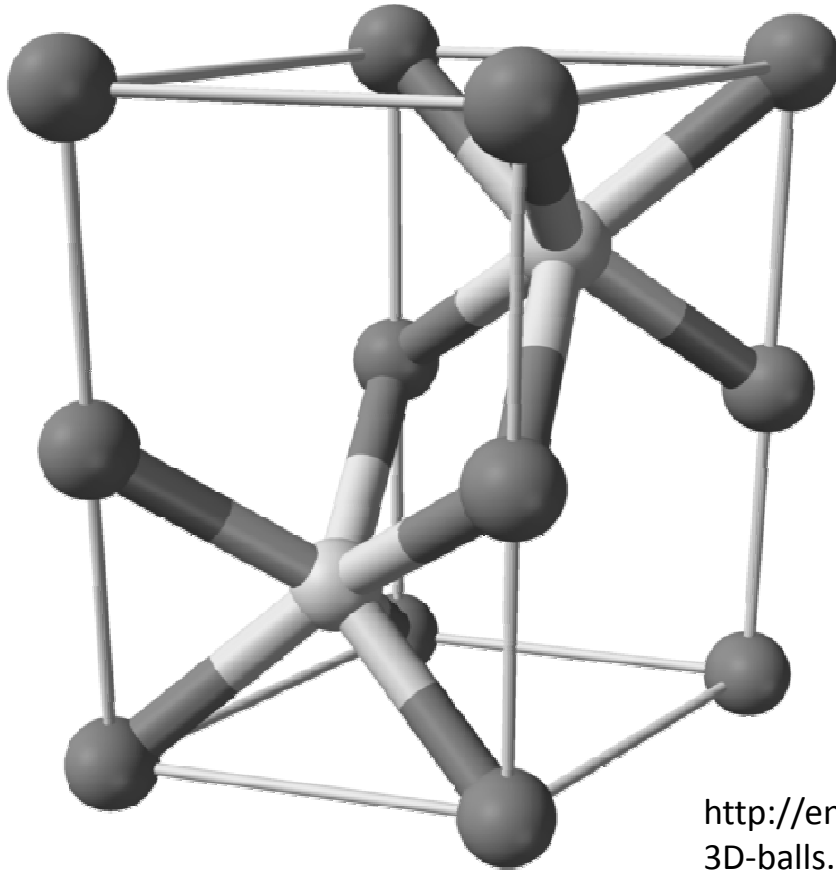
Structure – WC (MN)



<http://www.ls-carbide.com/About%20tungsten%20carbide.html>



Structure – NiAs (MN)



[http://en.wikipedia.org/wiki/File:Iron\(II\)-sulfide-unit-cell-3D-balls.png](http://en.wikipedia.org/wiki/File:Iron(II)-sulfide-unit-cell-3D-balls.png)

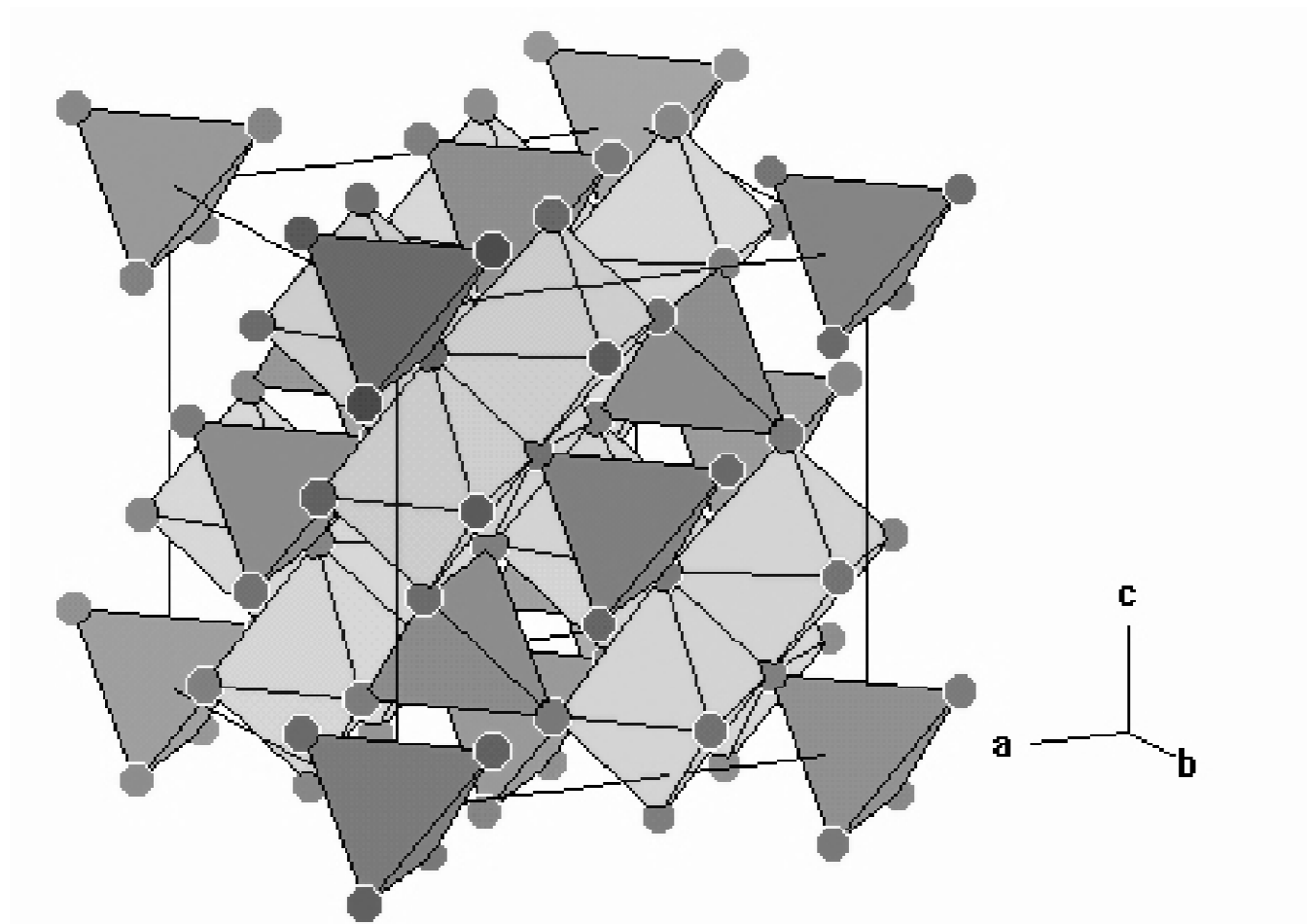


***Ab initio* method details**

- Vienna Ab initio Simulation Package (VASP)
- Ultra-soft Vanderbilt pseudo potentials (US-PP)
- Local-density approximation (LDA) and general gradient approximation (GGA) were used and mean values used
- kinetic energy cutoff value: 450 eV
- The electronic self-consistent loops converge below 10^{-4} eV/atom
- $12 \times 12 \times 12$ Monkhorst-Pack mesh, and denser mesh for DOS
- Murnaghan equation of state used for equilibrium lattice constant
- Three independent strains applied and a set of three equations solved for elastic constants

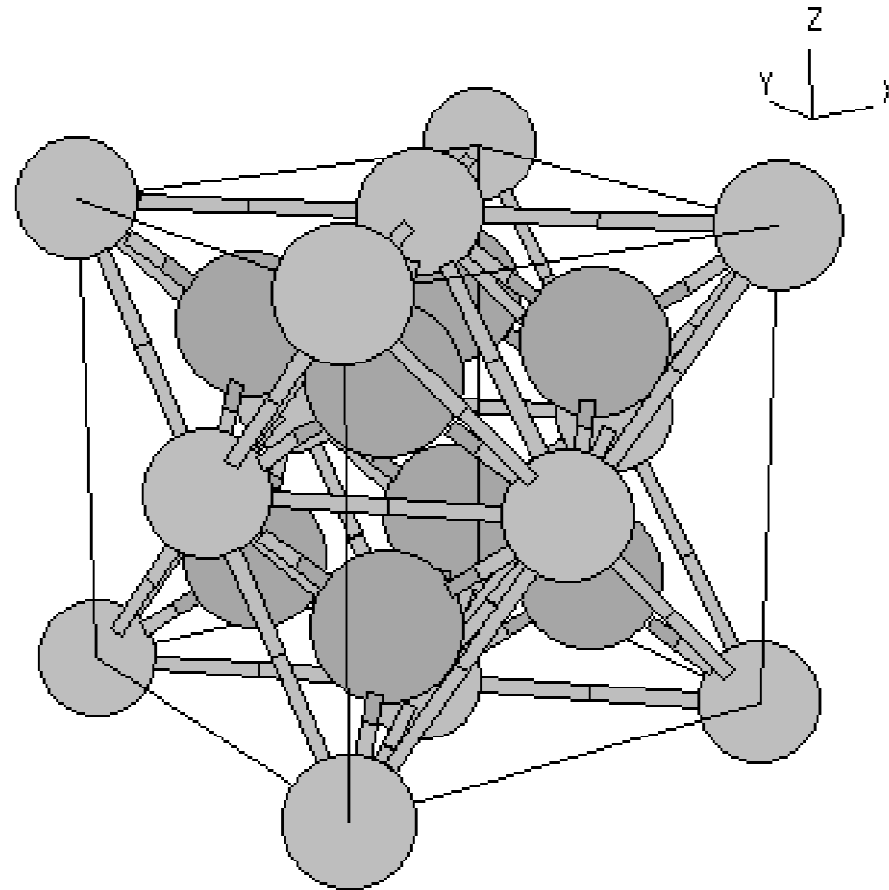


Structure – spinel (M_3N_4)



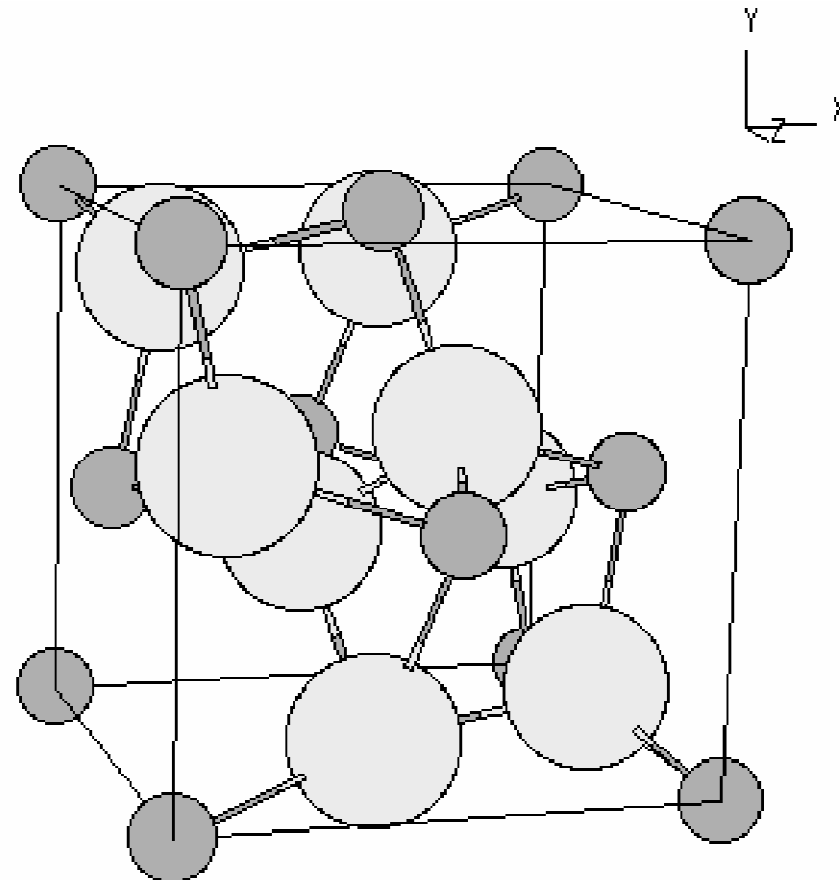


Structure – fluorite (MN_2)



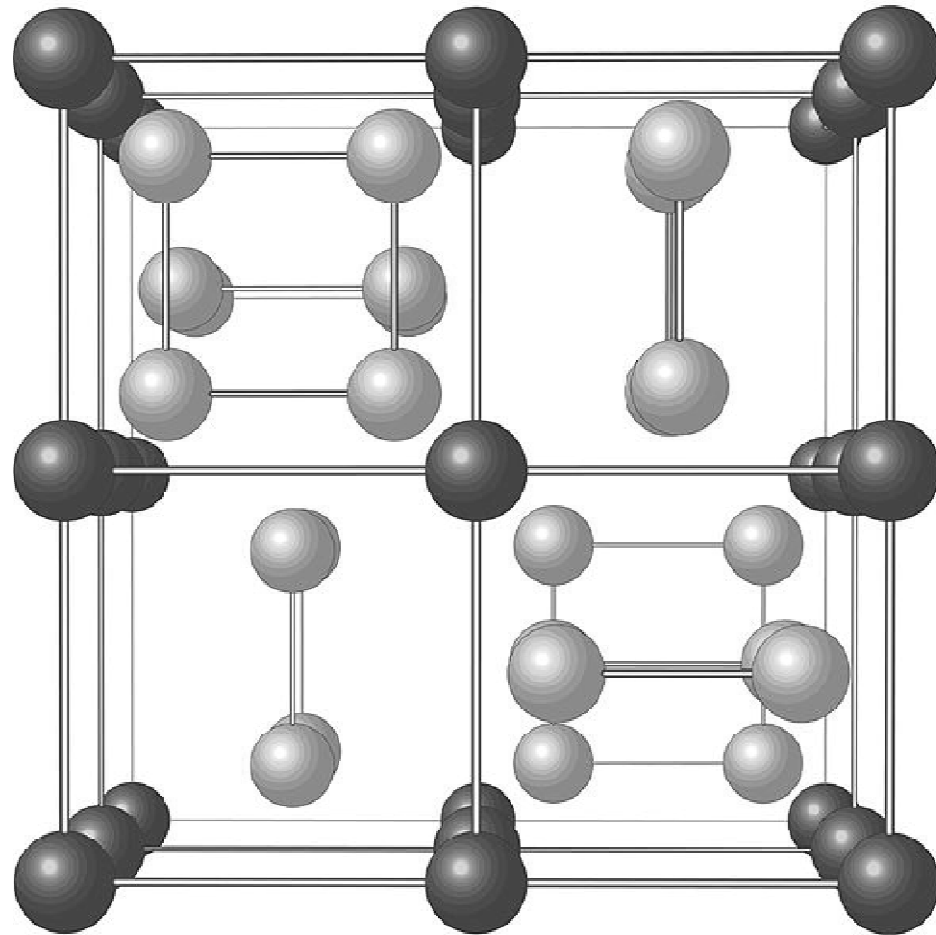


Structure – pyrite (MN_2)



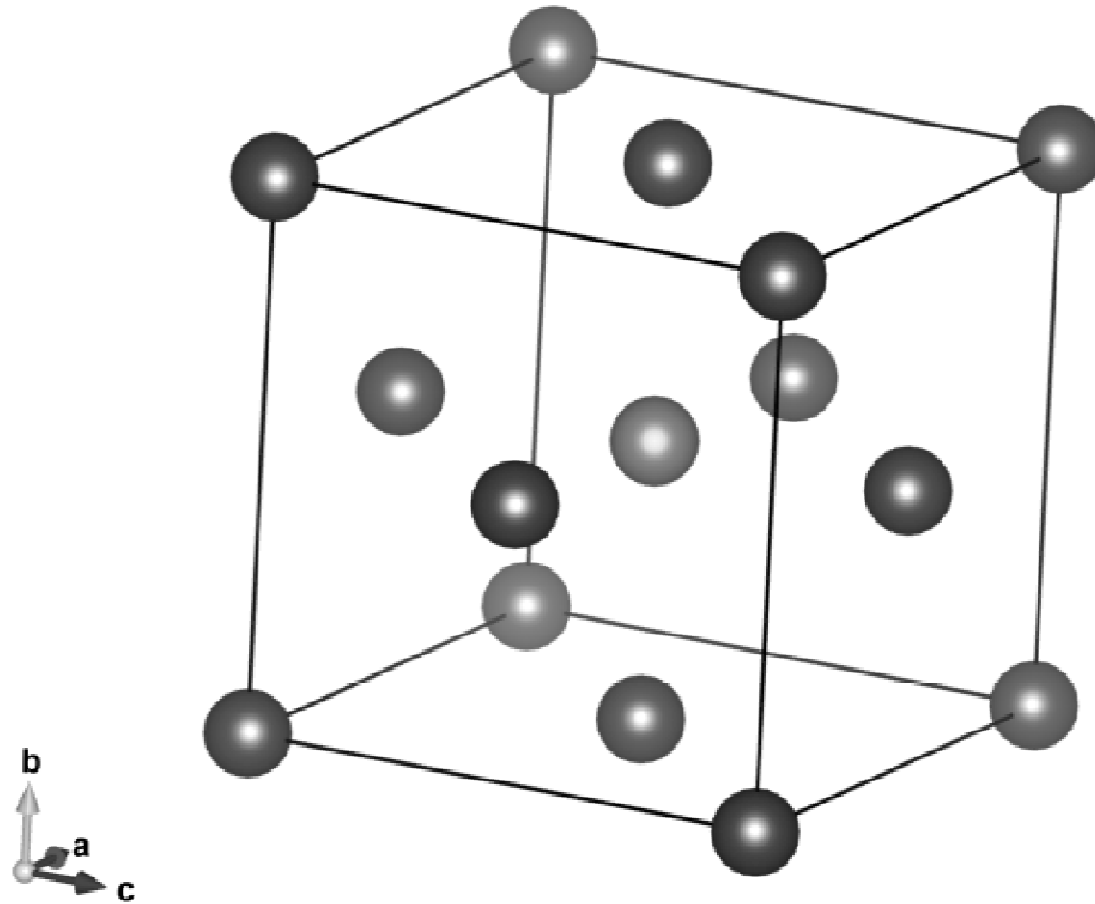


Structure – skutterudite (MN_3)



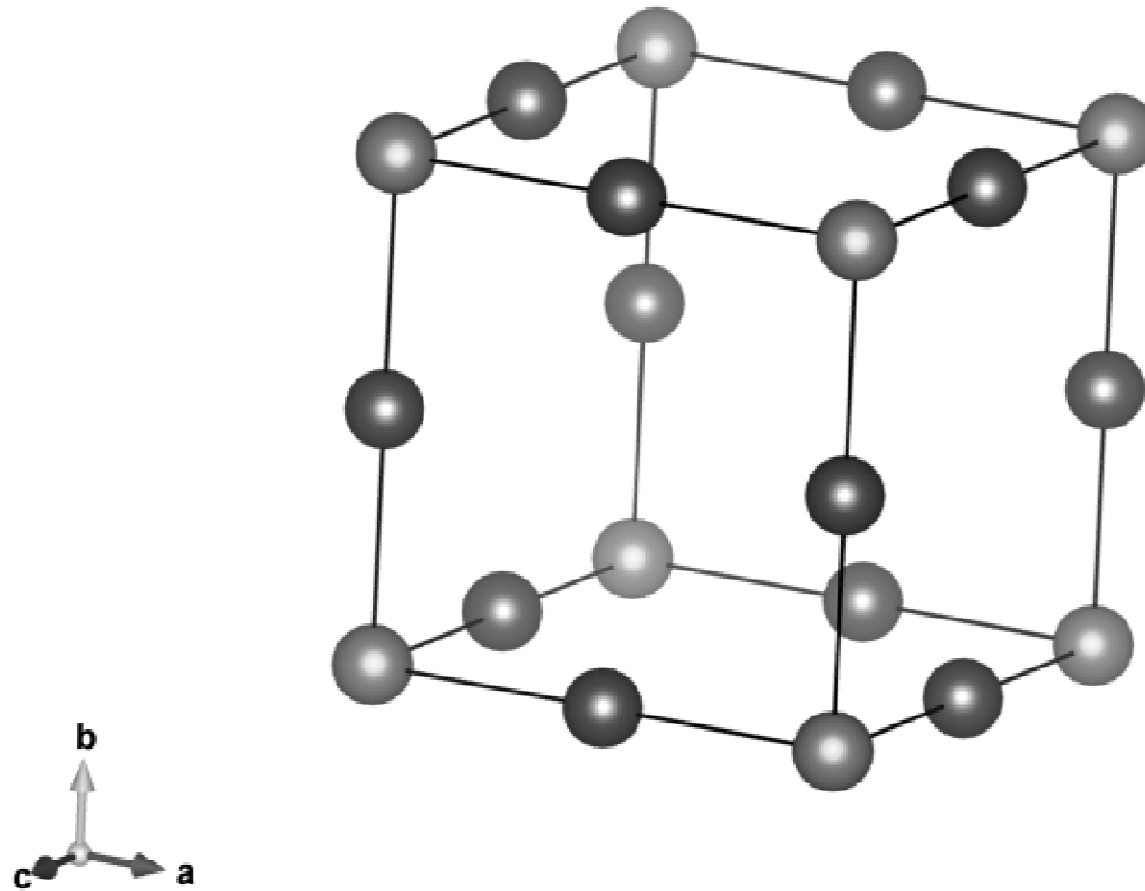


Structure – M_4N



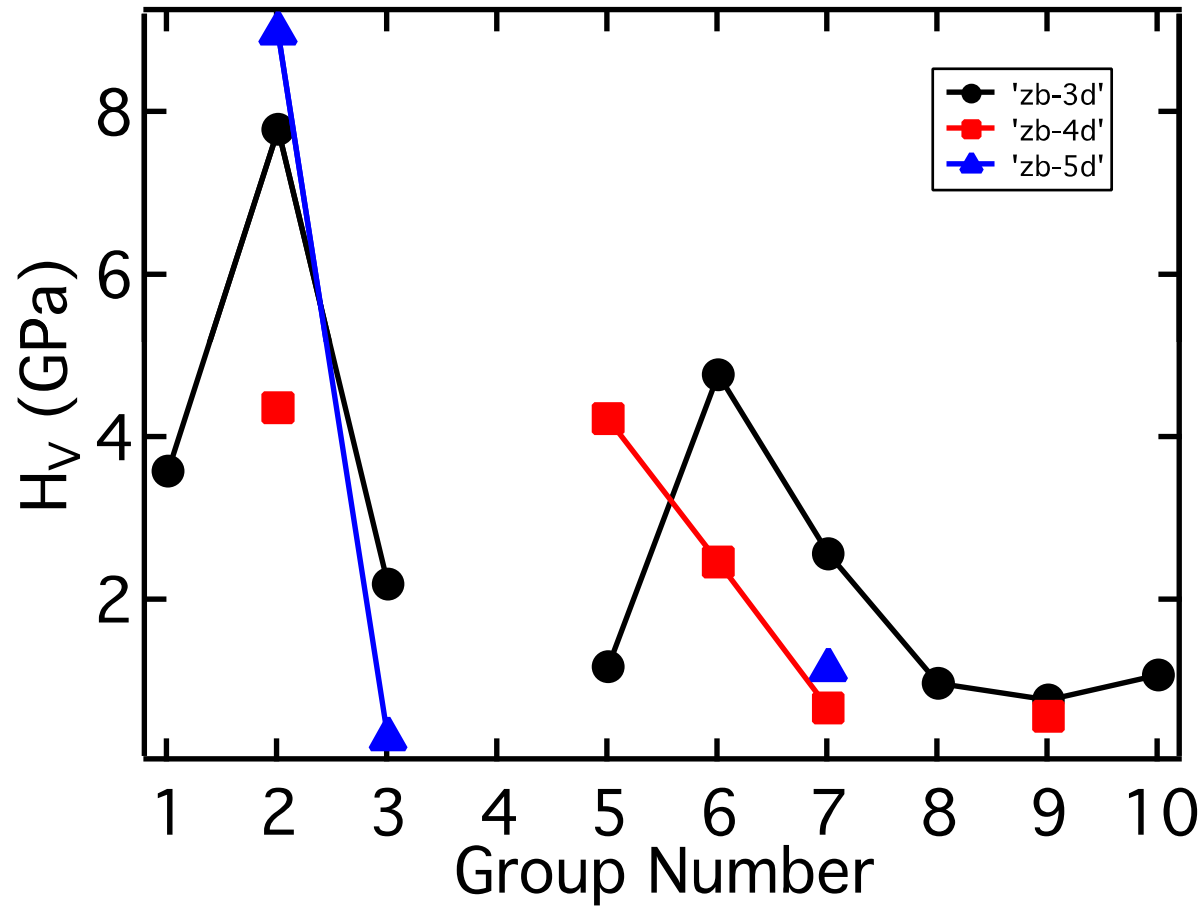


Structure – anti-ReO₃ (M₃N)



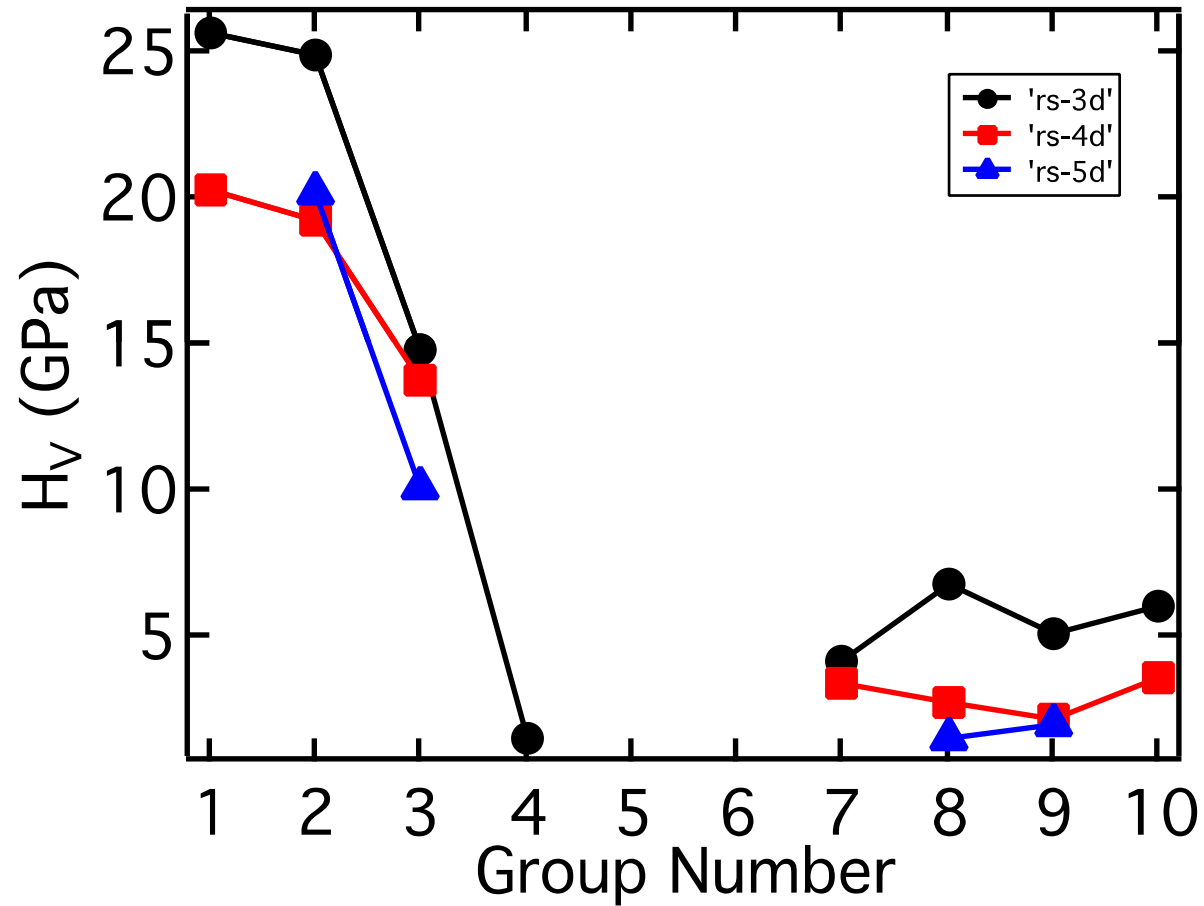


Structure - zincblende (MN)



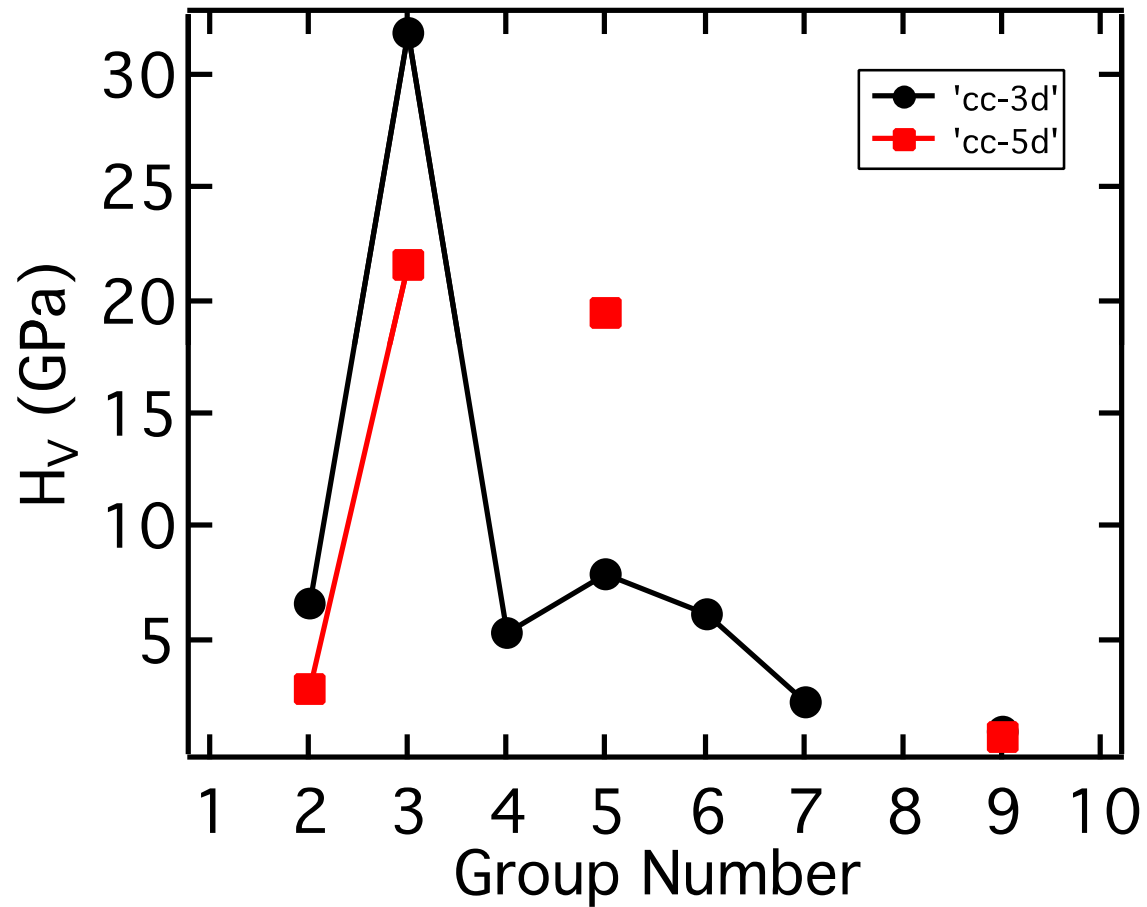


Structure - rocksalt (MN)



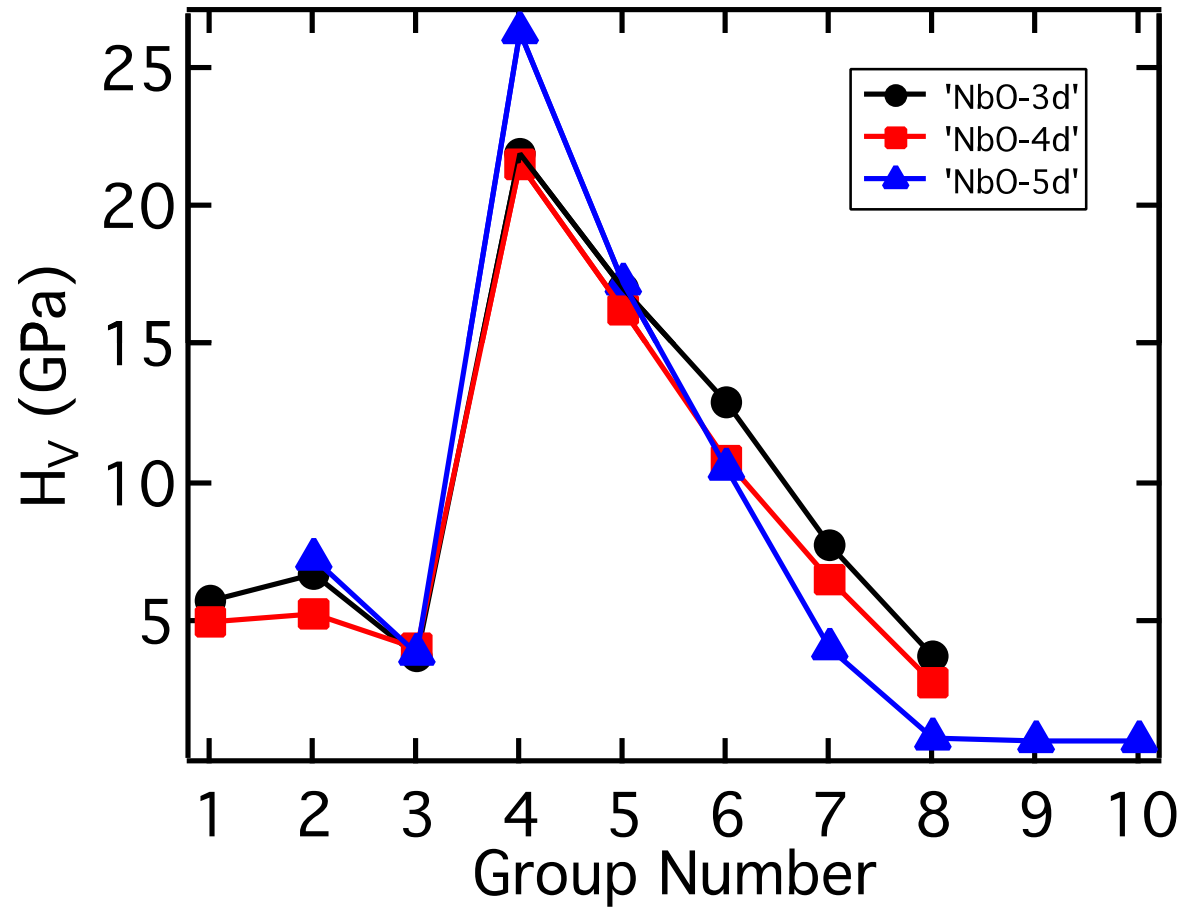


Structure - cesium chloride (MN)



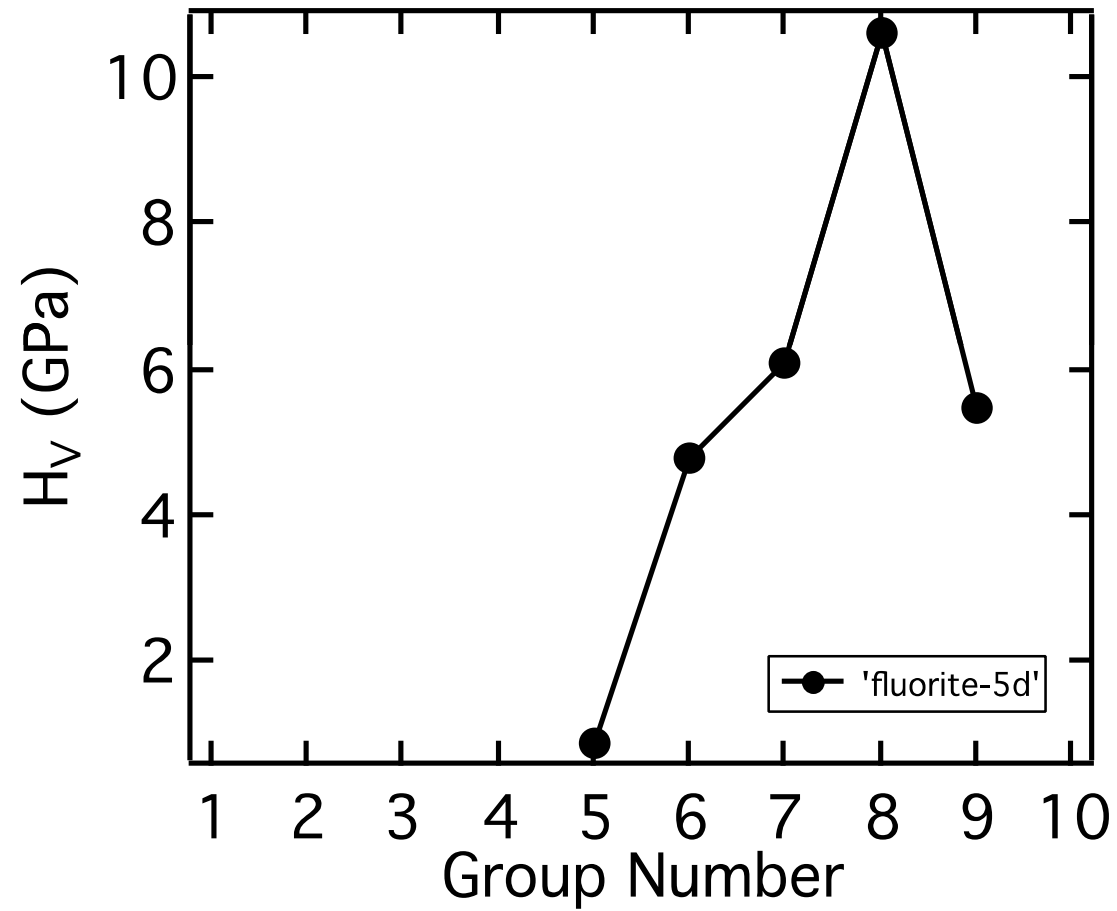


Structure - NbO (MN)



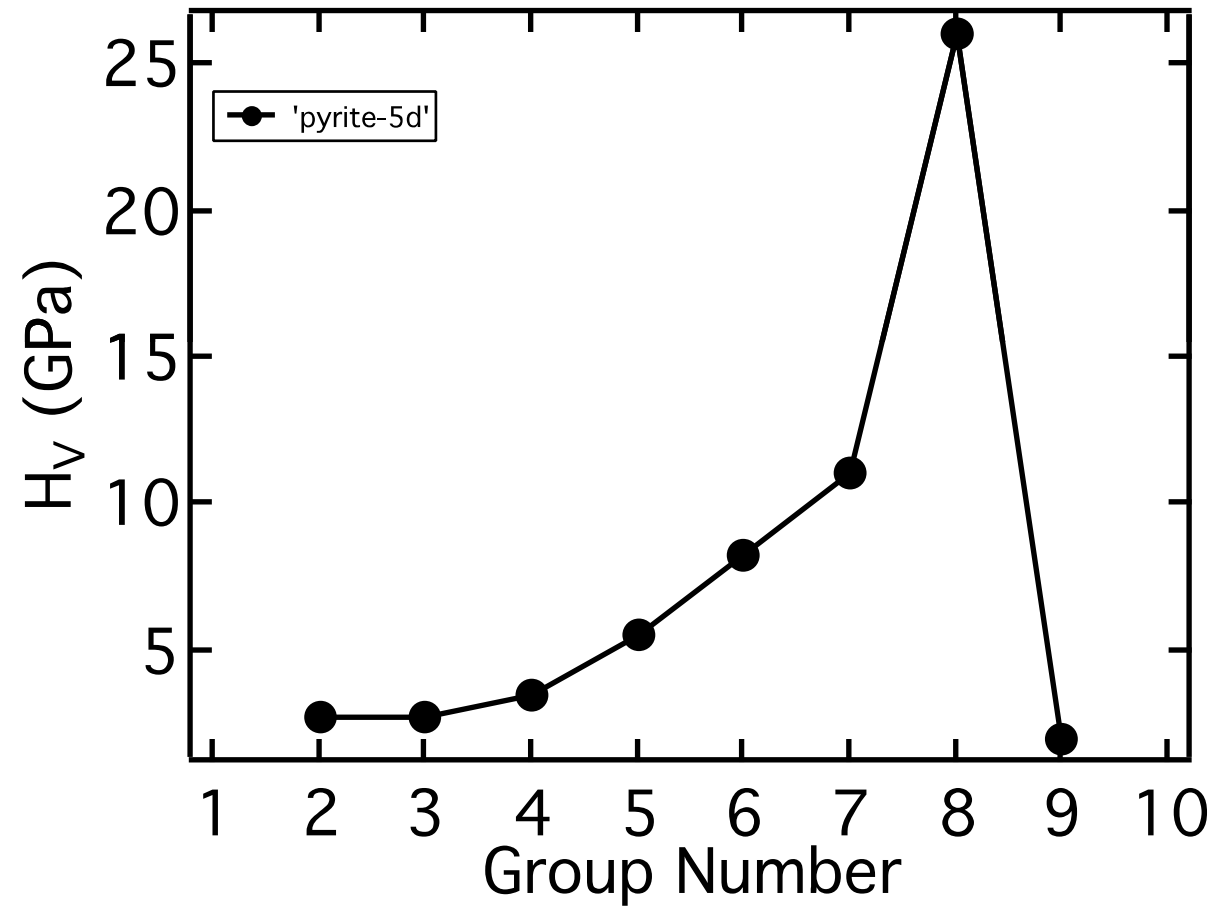


Structure - fluorite (MN_2)



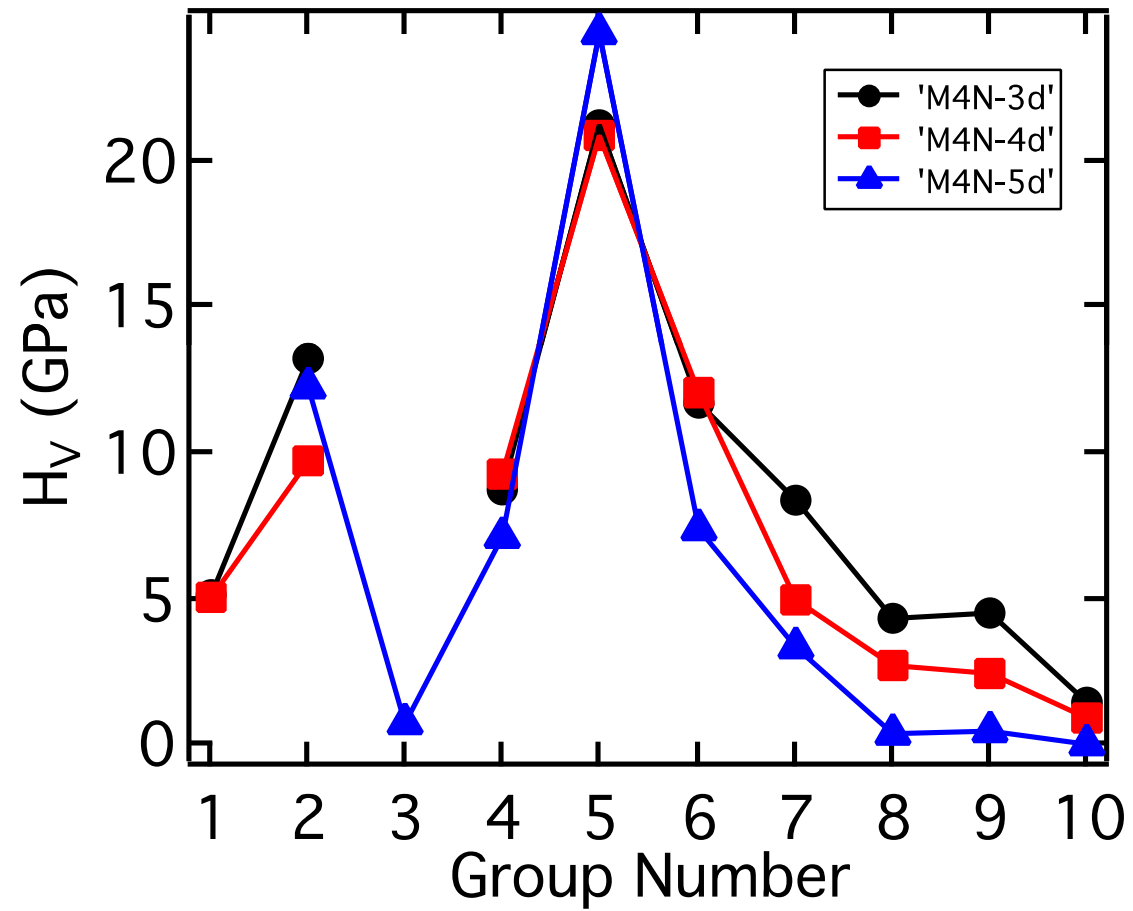


Structure - pyrite (MN_2)



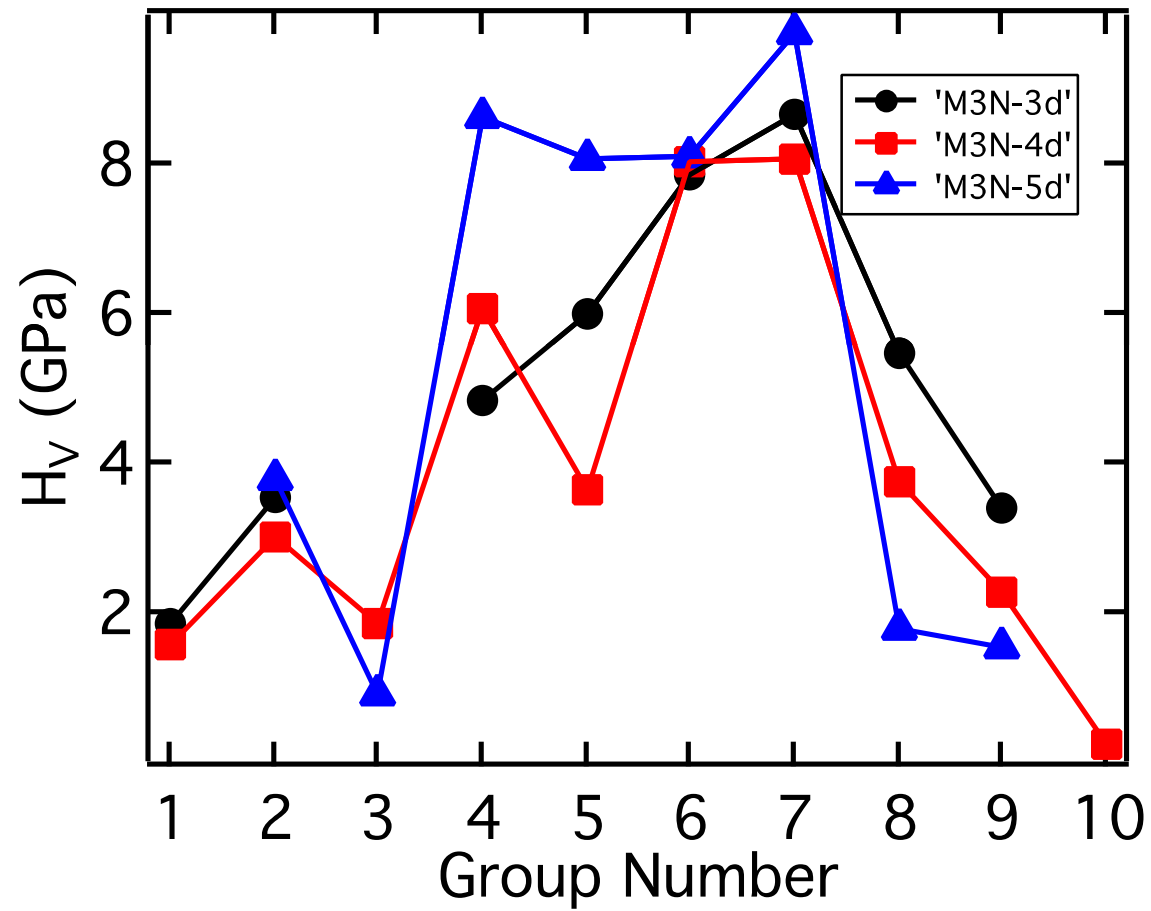


Structure - M_4N



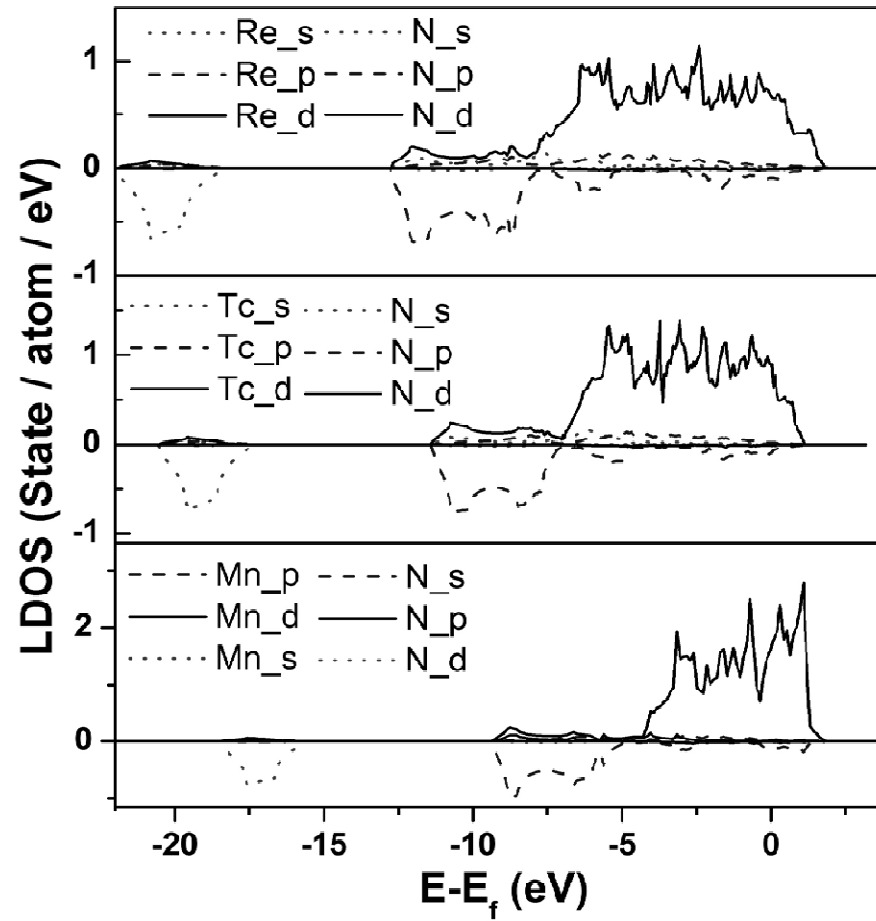


Structure - anti-ReO₃ (M₃N)





LDOS of M_4N





Value of *ab initio* method



- Powerful predictive tool to calculate properties of materials
- Fully first principles ==>
 - (1) no fitting parameters, use only fundamental constants (e, h, m_e , c) as input
 - (2) Fully quantum mechanical for electrons
- Thousands of materials properties calculated to date
- Used by biochemists, drug designers, geologists, materials scientists, and even astrophysicists!
- Evolved into different varieties for ease of applications
- Awarded chemistry Nobel Prize to W. Kohn and H. Pople 1998



Thank you!